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MAGNITUDE: YIELD RELATIONSHIP AT VARIOUS NUCLEAR TEST SITES --- A MAXIMUM-LIKELIHOOD APPROACH USING HEAVILY CENSORED EXPLOSIVE YIELDS

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development of a procedure capable of making full use of such censored information would seem very timely and necessary

In section I of this report, we present a maximum-likelihood regression scheme, "MLE-CY", which takes all the censored yields into account to refine the estimated m_b : yield relationship. This regression routine is very similar to the maximum-likelihood estimator used in computing the optimal network m_b values based on the censored station amplitude measurements due to clipping and to non-detection. In the non-censored case, it gives results identical to those derived by the standard least-squares method. Applications of this scheme to the explosions from several test sites of different geology show that it is a superior procedure, as compared to the conventional least-squares approach. The same algorithm can be applied to other magnitude measurements such as M_S , Pcoda, $m_b(L_g)$, M_o , RMS L_g and DOB etc.

We have also conducted a systematic analysis of the magnitude: yield relationship at five major test sites using miscellaneous unclassified magnitudes. (A classified annex using the official m_b values will be furnished separately.)

Several noteworthy results are summarized here:

- Including the censored yields in the regression does improve the accuracy of the estimates. In reality, both the magnitude and the yield measurements are subject to error. Pending the determination as to which of the two extreme hypotheses, namely $\sigma(m_b)/\sigma(Y)=0$ and $\sigma(m_b)/\sigma(Y)=\infty$, is closer to the real situation, we also included the results based on Ericsson's method with various $\sigma(m_b)/\sigma(Y)$. As expected, we can see the smooth transition of estimated parameters (i.e., the slope and the intercept) as $\sigma(m_b)/\sigma(Y)$ varies. Thus the censored cases with non-trivial $\sigma(m_b)/\sigma(Y)$ values could be "interpolated". Our maximum-likelihood regression scheme and Ericsson's method represent two different directions in extending the standard least squares.
- [2] For Shagan events, Ringdal's $RMS L_g$ provides the smallest scatter around the calibration curve, provided that low-yield events with $m_b(RMS L_g) < 5.5$ or yield < 40KT are excluded. Geotech's GLM method gives network m_b values better than almost all other magnitudes based on the teleseismic P waves and $\log(\Psi_m)$, in terms of both the yield estimation and the m_b scaling against Ringdal's $RMS L_g$. For all five test sites we have compared, m_b measurements reported by ISC and NEIS are piased high systematically at low yields.
- [3] A direct estimation of the test site bias suggests that Nuttli's (1987, 1988) Degelen puzzle could be invalid simply because of the relatively poorer quality m_b (ISC) used. Our data indicate that Shagan River Test Site is more efficient in exciting teleseismic P waves than Degelen Mountain, consistent with our previous modeling study. Also, the test site bias is yield dependent, in agreement with other observational study.
- [4] We present an alternative approach to derive the m_b adjustment converting cratering shots to contained explosions of the same yield. The correction derived by this approach seems to match that by the multichannel deconvolution method rather well.
- [5] Degelen Mountain is the only test site that has a decreasing log(P_{max}/P_a) and log(P_b/P_a) with increasing yields. It is also the only test site for which the phase "a" (i.e., zero-crossing to first peak) shows the smallest scatter around the calibration curve, as compared to the phases "b" (i.e., first peak to first trough) and "max" (i.e., max peak-to-trough or trough-to-peak in the first 5 seconds). Both the mountainous topography (which causes complex pP interference) as well as the testing practice (e.g., the relatively shallow and abnormal shot depths) could be responsible. At Shagan River, the phase "b" has the smallest scatter around the calibration curve. These observations confirm the conjecture (DARPA, 1981) that in a proper environment the first cycle could give better results than does "max" phase.
- [6] The scale depth for Konystan explosions is 146 ± 1 meters, and the depth of burial [DOB] is roughly proportional to the quartic root of the yield, rather than the cubic root as frequently cited at NTS. This empirical scaling rule is applicable to Shagan River region, but not Degelen Mountain. For Konystan and Shagan regions, the yields estimated using depth scaling have accuracy comparable to those using m_b .

EXECUTIVE SUMMARY

Conventional methods for estimating underground explosion yields from seismic recordings are based on the use of some appropriate "magnitude:yield" relationship. One of the most important parameters used to characterize the seismic signature of an underground explosion is the body-wave magnitude, m_b . Thus obtaining an unbiased measurement of m_b (or auxiliarily M_S , Pcoda, $m_b(L_g)$, M_o , and RMS L_g values) is obviously a key step in estimating the yield. During the past decade, the m_b which is averaged over a well-distributed global network and which incorporates the maximum-likelihood technique into the inversion scheme has become widely accepted as a means to obtain m_b estimates that avoid bias due to the detection threshold characteristics of individual network stations.

Recently Soviet seismologists have published descriptions of 96 nuclear explosions conducted from 1961 through 1972 at the Semipalatinsk Test Site, in Eastern Kazakhstan. With the exception of releasing news about their "peaceful nuclear explosions" [PNE], the Soviets have never before published such a body of information. However, out of the 72 Degelen events with announced yields, only 9 events or 12.5% were of "known" yields. The remaining were either left censored (66.7%) or bounded (20.8%). Similar heavy-censoring pattern can be found for other test sites. Thus the development of a procedure capable of making full use of such censored information would seem very timely and necessary.

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- the smooth transition of estimated parameters (i.e., the slope and the intercept) as $\sigma(m_b)/\sigma(Y)$ varies. Thus the censored cases with nontrivial $\sigma(m_b)/\sigma(Y)$ values could be "interpolated". Our maximum-likelihood regression scheme and Ericsson's method represent two different directions in extending the standard least squares.
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- [3] A direct estimation of the test site bias suggests that Nuttli's (1987, 1988) Degelen puzzle could be invalid simply because of the relatively poorer quality m_b (ISC) used. Our data indicate that Shajan River Test Site is more efficient in exciting teleseismic P waves than Degelen Mountain, consistent with our previous modeling study. Also, the test site bias is yield dependent, in agreement with other observational study.
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SECTION I

MAXIMUM-LIKELIHOOD MAGNITUDE: YIELD REGRESSION WITH CENSORED INFORMATION

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I.O ABSTRACT

Officially announced yields of underground nuclear explosions are often truncated or incomplete. So far such censored information has not been fully utilized in the determination of m_b :yield calibration curves. In this study, we present a maximum-likelihood regression scheme which takes all the censored yields into account to refine the empirical m_b :yield relationship. Preliminary applications of this scheme to the explosions from several test sites of different geology show that it is a superior procedure, as compared to the conventional least-squares approach. A joint and direct inversion reveals that the m_b bias between Eastern Kazakhstan, U.S.S.R., and Nevada Test Site, U.S., is about 0.40 and 0.44 at 10KT and 100KT, respectively. The same algorithm can be applied to other magnitude measurements such as M_S , $P \cos m_b(L_g)$, M_o and RMS L_g values etc.

1.1 INTRODUCTION

Conventional methods for estimating underground explosion yields from seismic recordings are based on the use of some appropriate "magnitude:yield" relationship. One of the most important parameters used to characterize the seismic signature of an underground explosion is the body-wave magnitude, m_b . Thus obtaining an unbiased measurement of m_b (or similarly M_S , Pcoda, $m_b(L_g)$, M_o , or RMS L_g values etc.) is obviously a key step in estimating the yield. There are already many publications which describe different procedures to infer better estimates of m_b : e.g., Douglas (1966), von Seggern (1973), Ringdal (1976), von Seggern and Rivers (1978), Christoffersson and Ringdal (1981), Blandford and Shumway (1982), Blandford et al. (1983), Lilwall (1986), McLaughlin et al. (1988b), Lilwall et al. (1988), and most recently, Jih and Shumway (1989). During the past decade, the m_b which is

m_b:Yield Regression with Censored Data

averaged over a well-distributed global network and which incorporates the maximum-likelihood technique into the inversion scheme has become widely accepted as a means to obtain m_b estimates that avoid bias due to the detection threshold characteristics of individual network stations.

Officially announced yields of underground nuclear explosions are often truncated or incomplete. In general there are four types of announced yields available:

- [0] W is known as y_0 KT (e.g., the Pahute Mesa event KNICKERBOCKER [5/26/67] had a yield of 71KT).
- [1] W is left censored, *i.e.*, the exact value of W is known only to be less than a certain level t_1 (e.g., the Konystan, U.S.S.R., event on [8/26/72] had a yield less than 20KT).
- [2] W is right censored, *i.e.*, the exact value of W is known only to be larger than a certain level t₂ (*e.g.*, the Pahute Mesa event HANDLEY [3/26/70] had a yield slightly larger than 1000KT), and
- [3] W is known only to lie between two bounds, t_a and t_b (e.g., the Yucca Flat event FLASK [5/26/70] had a yield between 20 and 200KT).

Observations of types 1 through 3 are censored. Regression with right-censored data is an important topic in survival analysis as well as in quality control (Schmee and Hahn, 1979; Aitkin, 1981; and many others), while some biochemical and environmental studies involving the monitoring of toxic material or water quality have inevitably led to the analysis of leftcensored data (e.g., Gleit, 1985; Shumway et al., 1989; and many others). Both leftcensored and right-censored station recordings due to the ambient noise and signal clipping are crucial in the estimation of network m_b (Ringdal, 1976; von Seggern and Rivers, 1978; Blandford and Shumway, 1982; Jih and Shumway, 1989). For yield determination, likewise, neglecting any of the three aforementioned censoring patterns could cause serious bias, not to mention the waste of useful information. For instance, recently Soviet seismologists (Bocharov et al., 1989) have published descriptions of 96 nuclear explosions conducted from 1961 through 1972 at the Semipalatinsk Test Site, in Eastern Kazakhstan (Vergino, 1989). With the exception of releasing news about their "peaceful nuclear explosions" [PNE] (Nordyke, 1974), the Soviets have never before published such a body of information. However, out of the 72 Degelen events with announced yields, only 9 events or 12.5% were of type 0. The remaining were either left censored (66.7%) or bounded (20.8%). The U.S. announced yields (Springer and Kinaman, 1971 and 1975) reflect a very similar heavy-censoring pattern. Although many authors have approached the subject of determining yield from m_b or other magnitude measures in a systematic way (e.g., Evernden, 1967; Ericsson, 1971a, 1971b; Springer and Hannon, 1973; von Seggern, 1977; Dahlman and Israelson, 1977; Marshall et al., 1979; Nuttli, 1986a, 1986b, 1988; Heasler et al., 1988; etc.), the huge amount of censored information has never been fully utilized in the determination of m_b : yield calibration curves.

m,:Yield Regression with Censored Data

In this study, we present a maximum-likelihood regression scheme which takes all the censored yields into account to refine the estimated m_b :yield relationship. This regression routine is very similar to the maximum-likelihood estimator used in computing the optimal network m_b values based on the censored station amplitude measurements due to clipping and to non-detection in the non-censored case, it gives identical results as that derived by the standard least-squares method. The same algorithm can be applied to other magnitude measurements such as M_S , Pcoda, $m_b(L_g)$, M_o and RMS L_g values etc.

1.2 MAXIMUM-LIKELIHOOD YIELD ESTIMATOR

The problem of estimating the yield of an explosion from the seismic magnitude has been handled traditionally using the linear model

$$X = \alpha + \beta \log(W) + v = \alpha + \beta Y + v$$
 [1]

where X is the measured magnitude, m_b , α and β are intercept and slope estimators, W is the yield in kiloton [KT], and v is an error term. v is assumed to be a Gaussian random variable with mean zero and standard deviation σ . The linear or piecewise-linear relationship between the log(yield) and the log(amplitude) is based on both observational study and theoretical prediction (e.g., Mueller and Murphy, 1971; von Seggern and Blandford, 1972; Murphy, 1977).

One may then collect a number of "calibration events", estimating α and β by least squares using a number of known yields and measured magnitudes. This classical calibration approach leads to predicting a future log-yield Y at $m_b = \hat{X}$ by inverting equation [1], i.e.,

$$\hat{\mathbf{Y}} = \frac{\hat{\mathbf{X}} - \hat{\mathbf{\alpha}}}{\hat{\mathbf{B}}}$$
 [2]

The geometrical interpretation of "regressing X on Y" is that the $(\hat{\alpha}, \hat{\beta})$ thus estimated would be the optimal solution that minimizes the sum of the squared magnitude residuals, $\sum (X - \hat{\alpha} - \hat{\beta}Y)^2$ (and hence the name of "m-regression"). Implicitly, an assumption is been made that the independent variable Y has nearly perfect accuracy and precision as compared to X.

Alternately, one can estimate κ and λ in the inverse regression model

$$Y = \log(W) = \kappa + \lambda X + v'$$
 [3]

and then predict a future log yield directly as

$$\hat{\mathbf{Y}} = \hat{\mathbf{x}} + \hat{\lambda}\,\hat{\mathbf{X}} \tag{4}$$

Likewise, this so-called "Y-regression" approach implicitly assumes that X has perfect accuracy and precision. The optimal estimates $(\hat{\kappa}, \hat{\lambda})$ are the ones that would minimize the sum of the squared log yield residuals, $\sum (Y - \hat{\kappa} - \hat{\lambda}X)^2$. Thus either the yield or the magnitude must be regarded as error-free independent variable in these two models. In reality, both the m_b and the yield measurements are subject to error. At NTS, where the yields can be measured using the radiochemical method with a precision better than that of the seismic method, $\sigma(m_b) >> \sigma(\log \text{ yield})$ could be a reasonable assumption. This may not be the case in general, however. Note that [3] can be rewritten in a form similar to [1]:

$$X = \alpha + \beta Y + v''$$
 [3']

with the transformations $\alpha = -\kappa/\lambda$, $\beta = 1/\lambda$.

m,: Yield Regression with Censored Data

Now suppose there are n_0 , n_1 , n_2 , and n_3 events for each type, respectively. We will derive the maximum-likelihood formulation for Y-regression model first (Equations [3] and [3']). The conditional likelihood function of the censored observations (\mathbf{y}_0 , \mathbf{t}_1 , \mathbf{t}_2 , \mathbf{t}_a , \mathbf{t}_b) given the intercept α , slope β , and the standard deviation σ of error in log yield is

$$L (y_0, t_1, t_2, t_a, t_b \mid \alpha, \beta, \sigma) = \prod_{j=1}^{n_0} P(Y_j = y_{0j} \mid \alpha, \beta, \sigma) * \prod_{j=1}^{n_1} P(Y_j < t_{1j} \mid \alpha, \beta, \sigma) *$$

$$\prod_{j=1}^{n_2} P(Y_j > t_{2j} \mid \alpha, \beta, \sigma) * \prod_{j=1}^{n_3} P(t_{aj} < Y_j < t_{bj} \mid \alpha, \beta, \sigma)$$
[5]

and the log-likelihood function is

In L (
$$y_0$$
, t_1 , t_2 , t_a , t_b | α , β , σ) = $-\frac{n_0}{2} \ln(2\pi\sigma^2) - \frac{1}{2\sigma^2} \sum_{j=1}^{n_0} (y_{0j} - \frac{x_{0j} - \alpha}{\beta})^2 + \frac{\sum_{j=1}^{n_1} \ln \Phi(z_{1j}) + \sum_{j=1}^{n_2} \ln \Phi(-z_{2j}) + \sum_{j=1}^{n_3} \ln [\Phi(z_{bj}) - \Phi(z_{aj})]}$ [6]

where x the seismic magnitudes; $z_i \equiv \frac{\alpha + \beta t_i - x_i}{\beta \sigma}$ for i = 1j, 2j, aj, and bj; $\phi(u) \equiv \frac{1}{\sqrt{2\pi}} \exp(\frac{-u^2}{2})$ and $\Phi(u) \equiv \int_{-\infty}^{u} \phi(x) dx$ are the probability density function [p.d.f.] and the cumulative distribution function [c.d.f.] of the standard normal N(0,1), respectively; and y_0 , t_1 , t_2 , t_a , and t_b are the collection of announced yields. The specific form of the rightmost term in equation [6] reveals the necessity of treating the type 3 censored data as a separate class rather than considering each of type 3 event as two separate events of type 1 and 2.

Solving $\frac{\partial \ln L}{\partial \sigma} = 0$ implies immediately that the maximum-likelihood solution of σ must satisfy the following necessary condition:

$$\sigma(\log \text{ yield})^{2} = \frac{\sum_{j=1}^{n_{0}} (y_{0j} - \frac{x_{0j} - \alpha}{\beta})^{2}}{n_{0} + \sum_{j=1}^{n_{1}} \frac{\phi(z_{1j})}{\Phi(z_{1j})} z_{1j} - \sum_{j=1}^{n_{2}} \frac{\phi(z_{2j})}{\Phi(-z_{2j})} z_{2j} + \sum_{j=1}^{n_{3}} \frac{\phi(z_{bj})z_{bj} - \phi(z_{aj})z_{aj}}{\Phi(z_{bj}) - \Phi(z_{aj})}}$$
[7]

 (α, β, σ) can be solved iteratively with the Expectation Maximization (EM) algorithm (Dempster *et al.*, 1977) as follows:

Initialization Step:

Infer the initial guess of the unknown parameters, (α, β, σ) , from the standard regression with the type 0 data alone.

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• E Step:

Replace the censored yields by their conditional expectations based on the current estimate of the parameters.

• M Step:

Recompute σ with [7] and update α and β by regressing with the refined pseudo observations computed in the E step. Then repeat steps E and M until α , β , and σ converge.

Dempster et al. (1977) proved that such iterative procedure guarantees the monotonic increase of the likelihood function of the new estimate, which in turn guarantees the convergence of the whole procedure since the log-likelihood function defined in [6] is bounded above, say, by 0.

The following prerequisite mathematics are used in the E step. Let X be an arbitrary Gaussian random variable with mean μ and variance σ^2 , p.d.f. g, c.d.f. G, then

- E(X|X < a) = μ σ^2 g(a)/G(a),
- $E(X \mid X > a) = \mu + \sigma^2 g(a)/G(-a)$,
- E(X | a < X < b) = μ $\sigma^2[g(b)-g(a)]/[G(b)-G(a)]$.

The calculation of g(x) and G(x) can be accomplished easily by the following transformations: $g(x) = \phi(\frac{x-\mu}{\sigma})/\sigma$, $G(x) = \Phi(\frac{x-\mu}{\sigma})$, as was done in Equations [6]-[7].

If we regress the magnitudes on the log yields, Equation [7] becomes

$$\sigma(m_b)^2 = \frac{\sum_{j=1}^{n_0} (\alpha + \beta y_{0j} - x_{0j})^2}{n_0 + \sum_{j=1}^{n_1} \frac{\phi(z_{1j})}{\Phi(z_{1j})} z_{1j} - \sum_{j=1}^{n_2} \frac{\phi(z_{2j})}{\Phi(-z_{2j})} z_{2j} + \sum_{j=1}^{n_3} \frac{\phi(z_{bj}) z_{bj} - \phi(z_{aj}) z_{aj}}{\Phi(z_{bj}) - \Phi(z_{aj})}}$$
[8]

where
$$z_i \equiv \frac{\alpha + \beta t_i - x_i}{\sigma}$$
 for $i = 1j$, 2j, aj, and bj .

Essentially the same procedure can be used for both the m- and Y-regression models. The major difference in the M step is whether we regress Y on X (and then transform κ and λ to α and β) or regress X on Y to estimate α and β directly. The other minor difference is in the calculation of σ and z. The σ in [7] represents the standard deviation of the residual log yield, while the σ in [8] is actually that for the residual magnitude. For the m-regression model, $\sigma(m_b)$ in [8] is frequently used as a measure of goodness of fit. If the Y-regression model is used, $\sigma(m_b)$ can be computed as $\sigma(\log yield)^*\beta$. The 2σ uncertainty factor in yield is defined as $10^{**}(2\sigma/\beta)$ and $10^{**}(2\sigma)$ for the m- and Y-regression models, respectively. Recently the m-regression model has been given greater attention in the nuclear monitoring study, and hence examples and discussions in the subsequent sections will be limited to the m-regression model for brevity. If $n_1 = n_2 = n_3 = 0$, then both algorithms presented here

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reduce to the standard least-squares method, and σ in [7] and [8] becomes the simple RMS residuals in the usual sense.

1.3 ILLUSTRATIVE EXAMPLES

During the past several years, WWSSN (World-Wide Standard Seismograph Network) m_b database measured at Teledyne Geotech (TG) has been gradually expanded to 124 events, totaling 366 usable "a", "b", and "max" event phases (Blandford and Shumway, 1982; Blandford et al., 1983; McLaughlin et al., 1988b; Jih and Shumway, 1989; Jih et al., 1990a; 1990b). We have applied the maximum-likelihood network m_b estimator, GLM [General Linear Model] (Blandford and Shumway, 1982), to the complete data set consisting of 15,288 teleseismic magnitude measurements in the distance range from 20 degrees to 95 degrees at 127 stations to determine our best m_b values to date, which we denote as m_b (TG). The m_b (P_{max} ,TG) and m_b (P_b ,TG) of the events from the same test site are then fed to the maximum-likelihood m_b :yield regression scheme we just proposed to derive the optimal calibration curve. The resulting calibration curves are summarized as follow:

- (#1) $m_b(P_{\rm max}, {\rm TG}) = 3.747[\pm 0.075] + 0.857[\pm 0.034] \log(W)$ for NTS shots in high-coupling media; $\sigma = 0.091$; 95% confidence factor = 1.630; *i.e.*, we are 95% confident that the actual yield lies in the range from $Y_{\rm est}/1.630$ to $Y_{\rm est}^*1.630$. In this regression $(n_0, n_1, n_2, n_3) = (9,2,1,2).$
- (#2) $m_b(P_b, TG) = 3.484[\pm 0.089] + 0.866[\pm 0.040] log(W)$ for NTS shots in high-coupling media; $\sigma = 0.108$; 95% confidence factor = 1.775. $(n_0, n_1, n_2, n_3) = (9,2,1,2)$.
- (#3) $m_b(P_{\text{max}}, \text{TG}) = 3.659[\pm 0.022] + 1.008[\pm 0.018] \log(\text{W})$ for Sahara and NTS shots in granite; $\sigma = 0.032$; 95% confidence factor = 1.157; $(n_0, n_1, n_2, n_3) = (4,6,1,0)$ (cf. Table 1).
- (#4) $m_b(P_b, TG) = 3.348[\pm 0.028] + 1.040[\pm 0.022] log(W)$ for Sahara and NTS shots in granite; $\sigma = 0.037$; 95% confidence factor = 1.178; $(n_0, n_1, n_2, n_3) = (4,6,1,0)$ (cf. Table 1).
- (#5) $m_b(P_{\text{max}}, \text{TG}) = 4.110[\pm 0.062] + 0.892[\pm 0.039] \log(\text{W})$ at Eastern Kazakhstan; $\sigma = 0.093$; 95% confidence factor = 1.617. $(n_0, n_1, n_2, n_3) = (13,3,0,5)$.
- (#6) $m_b(P_b, TG) = 3.837[\pm 0.059] + 0.924[\pm 0.037] log(W)$ at Eastern Kazakhstan; $\sigma = 0.091$; 95% confidence factor = 1.571. $(n_0, n_1, n_2, n_3) = (13,3,0,5)$.

Although the formulae (#1) through (#6) are preliminary, there are a few observations worth noting. First, the slope in (#1) matches Murphy's (1977) theoretical prediction, 0.85,

 $^{^{19}}$ events of type 0: BILBY, SHOAL, HANDCAR, REX, CHARTREUSE, PILEDRIVER, SCOTCH, BOXCAR, and BENHAM; 2 events of type 1: ALMENDRO and MAST; 1 event of type 2: HANDLEY; 2 events of type 3: CORDUROV and NASH. See Appendix (page 64) for the m_b values.

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rather well. Secondly, putting the representative explosions from various test sites recorded at a global network (such as WWSSN) into a single GLM inversion not only yields a consistent set of station corrections for global use, but it also provides a direct estimate of the m_b bias between any two test sites of interest. For instance, the m_b bias between Eastern Kazakhstan and NTS can be estimated easily from (#1) and (#5) as 0.40 and 0.436 magnitude unit at 10KT and 100KT, respectively. This value is very close to that based on some indirect methods using P_n velocity or surface waves (Evernden and Marsh, 1987), and slightly larger than that in Der *et al.* (1985) and Stewart (1988). It includes the combined effects of the net bias due to the clustering of stations on the focal sphere (McLaughlin, 1988) as well as the difference of Q, coupling, and pP interferences between two test sites.

In deriving (#3) and (#4), we have supplemented the French explosions in Hoggar Massif, south Algeria, with U.S. shots PILEDRIVER and SHOAL detonated at Climax Stock, Nevada. The French Test Site is in the volcanic terrain, apparently in an incipient rift zone (Duclaux and Michaud, 1970; Schock et al., 1972; Faure, 1972). The tof Hoggar Massif as estimated by Der et al. (1985) is 0.35 sec, which shows no significant difference in the attenuation from that of NTS (McLaughlin et al., 1988a). There exists fair agreement between U.S. and French granite shots in the yield-scaled peak values of acceleration, velocity, and displacement (Heuze, 1983). On the other hand, although the Semipalatinsk Test Site of U.S.S.R. has hard-rock geology as well, it is inappropriate to include the Soviet events in the same regression with French explosions unless care is taken in advance to correct for the test site bias. Table 1 lists the regression results using the least-squares (LS) and the maximumlikelihood estimator (MLE) along with the announced yields of U.S. and French tests in granite taken from Bolt (1976) and Stimpson (1988). The yield estimates in column "MLE" of Table 1 are predicted by formulae (#3) and (#4), respectively. Although the network m_b values we use are not corrected for the pP interference as suggested in Marshall et al. (1979), they fit the theoretical scaling rather well. The slope of the m_b : yield curve for this region is nearly 1 for these low-yield tests, consistent with an earlier study by Blandford and Shumway (1982) using fewer events. Because of the nearly ideal fit, the MLE changes the yields only slightly as estimated by the standard least squares method in this particular case.

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Table 1. Estimated Yield of French and U.S. Explosions in Granite								
Event	Announced	$m_b(P_{\text{max}}, TG)$	LS	MLE	$m_b(P_b,TG)$	LS	MLE	
	[KT]		[KT]	[KT]		[KT]	[KT]	
BERYL	>20.0	4.986	20.6	20.8	4.779	23.8	23.8	
CORUNDON	<20.0	4.214	3.5	3.6	3.900	3.4	3.4	
EMERAUDE	<20.0	4.569	7.9	8.0	4.263	7.6	7.6	
GRENAT	<20.0	4.766	12.4	12.6	4.497	12.7	12.7	
OPALE	<20.0	3.894	1.7	1.7	3.853	3.1	S. 1	
RUBIS	52.0	5.432	57.2	57.5	5.170	56.4	56.5	
SAPHIR	120.0	5.720	110.7	111.1	5.468	109.2	109.2	
TOURMALINE	<20.0	4.646	9.4	9.5	4.429	10.9	11.0	
TURQUOISE	<20.0	4.223	3.6	3.6	3.942	3.7	3.7	
SHOAL	12.2	4.739	11.7	11.8	4.455	11.6	11.6	
PILEDRIVER	56.0	5.436	57.7	58.0	5.195	59.7	59.7	

We have also derived the maximum-likelihood calibration curves using Nuttli's (1986a) $m_b(L_a)$ as well as Marshall's (1988) m_b values for NTS:

- (#7) Marshall's $m_b = 3.892[\pm 0.105] + 0.833[\pm 0.049] \log(W)$ for high-coupling material at NTS; $\sigma = 0.186$; 95% confidence factor = 2.799. Note that the mean slope, 0.833, is very close to that in (#1). $(n_0, n_1, n_2, n_3) = (19,13,1,27)$.
- (#8) Nuttli's $m_b(L_g) = 4.402[\pm 0.038] + 0.730[\pm 0.018] \log(W)$ for high-coupling material at NTS; $\sigma = 0.086$; 95% confidence factor = 1.717. $(n_0, n_1, n_2, n_3) = (22,14,1,30)$.
- (#9) Nuttli's $m_b(L_g) = 4.020[\pm 0.038] + 0.841[\pm 0.032] \log(W)$ for low-coupling material at NTS; $\sigma = 0.170$; 95% confidence factor = 2.536. $(n_0, n_1, n_2, n_3) = (14,41,0,24)$.

To illustrate the robustness of the present approach, we have tabulated below (Table 2) the best yield estimate of several often analyzed nuclear tests in hard rock computed using our formulae based on Marshall's, Nuttli's, and our magnitudes.

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Table 2. Comparison of Yield Estimate of 3 Granite Shots							
Events	RUBIS	SAPHIR	Kazakhstan 01/15/65				
Announced Yield	52KT	120KT	100-150KT				
Nordyke ^{*1}			125KT				
Dahlman and Israelson*2			110KT				
Marshall et al.*3	45.4KT	91.6KT	68.9KT				
	$[m_Q=5.97]$	$[m_O=6.29]$	$[m_Q=6.16]$				
Nuttli ^{*4} $m_b(L_g)$, Quadratic Fit	68KT	110KT	103KT				
Nuttli ^{*5} $m_b(L_g)$, Linear Fit	70KT	117KT	109KT				
	$[m_b(L_g) = 5.72]$	$[m_b(L_g) = 5.89]$	$[m_b(L_g) = 5.87]$				
Stimpson*6	68KT	127KT					
	$[m_b = 5.49]$	$[m_b = 5.70]$					
This Study, $m_b(P_{\text{max}}, TG)$	57.5KT	111.1KT	96.7KT				
	$[m_b(P_{\text{max}})=5.432]$	$[m_b(P_{\text{max}})=5.720]$	$[m_b(P_{\text{max}})=5.882]$				
This Study, $m_b(P_b,TG)$	56.5KT	109.2KT	112.9KT				
	$[m_b(P_b)=5.170]$	$[m_b(P_b)=5.468]$	$[m_b(P_b)=5.735]$				

^{*1)} Nordyke (1974): based on the crater size.

Patton (1988), Ringdal and Marshall (1989), Hansen *et al.* (1989), and Ringdal and Hansen (1989) confirmed that the L_g phase is very promising for use in yield estimation, as originally proposed by Nuttli (1986a, 1986b). Table 2 indicates that the yields estimated by our MLE regression scheme using our m_b measurements have equally good or better accuracy as does $m_b(L_g)$. The improvements over other conventional regression schemes can be attributed to two factors:

- [1] the maximum-likelihood magnitude:yield regression method presented in this study is superior to the conventional least-squares magnitude:yield regression, regardless of what magnitude is used; and
- [2] Geotech's GLM method results in a smaller bias in the network m_b estimates.

To explore the validity of the first claim, we analyzed 7 events with announced yields from the Shagan River Test Site (i.e., Balapan region) as listed in Table 3 using Marshall's

^{*2)} Dahlman and Israelson (1977): slope = 0.74.

^{*3)} Marshall et al. (1979): $m_Q = 4.23[\pm 0.15] + 1.05[\pm 0.06] \log(W)$ for salt and granite

^{*4)} Nuttli (1986a, b): $m_b(L_g) = 3.943 + 1.124 \log(W) - 0.0829 (\log(W))^2$ for $5.2 < m_b(L_g) < 6.7$

^{*5)} Nuttli (1986a, b): $m_b(L_a) \approx 4.307 + 0.765 \log(W)$ for $5.2 < m_b(L_a) < 6.7$

^{*6)} Stimpson (1988): $m_b = 4.08 + 0.77 \log(W)$ for hard rock

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(1987) m_b measurements and those of Sykes and Ruggi (1989).

When the standard least-squares (LS) is applied to Marshall's m_b values of the four events with known yields, the predicted yield of event [01/15/65] is 87.9KT. Once the remaining events of censored yields are added into our maximum-likelihood regression, the estimate becomes 92.0KT. If Sykes' m_b values were used instead, the yield estimate would change from 91.2KT (LS) to 94.9KT (MLE). Both cases show an obvious improvement relative to the announced yields by incorporating the censored yields into the regression. Furthermore, such improvement is not an isolated case. Out of 4 events with known yield, 3 events had significantly improved estimates.

	Table 3. Explosions at Shagan River Area with Announced Yield									
Date	Lat	Long	Depth	Yield	NEIS	Sykes	Marshall			
	[N]	(E)	[m]	[KT]	m _b	m_b	m _b			
650115	49.9350	79.0094	178	100-150	6.3	5.905	5.931			
680619	49.9803	78.9855	316	<20	5.5	5.350	5.354			
691130	49.9243	78.9558	472	125	6.0	5.954	6.048			
710630	49.9460	78.9805	217	<20	5.4	5.290	5.027			
720210	50.0243	78.8781	295	16	5.5	5.370	5.370			
721102	49.9270	78.8173	521	165	6.2	6.181	6.224			
721210	50.0270	78.9956	478	140	6.0	5.989	5.996			

[from Bocharov et al. (1989) and Vergino (1989)]

The maximum-likelihood calibration curves at Shagan River region using m_b values in Table 3 ($(n_0, n_1, n_2, n_3) = (4,2,0,1)$) are listed as follow:

(#10)

Marshall's $m_b = 4.476[\pm 0.090] + 0.741[\pm 0.052] \log(W)$ with 95% confidence factor 1.605 and σ 0.076.

(#11)

Sykes' $m_b = 4.525[\pm 0.096] + 0.698[\pm 0.054] \log(W)$ with 95% confidence factor 1.577 and σ 0.069.

(#12)

NEIS' $m_b = 4.807[\pm 0.164] + 0.614[\pm 0.093] \log(W)$ with 95% confidence factor 2.671 and σ 0.131.

Bocharov et al. (1989) and Vergino (1989) also listed the yields of Soviet nuclear explosions in Konystan (Murzhik) and Degelen regions. Using Marshall's m_b measurements, the

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maximum-likelinood calibration curves are:

(#13)

Marshall's $m_b = 4.535[\pm 0.045] + 0.768[\pm 0.039] \log(W)$ at Konystan; $\sigma = 0.069$; 95% confidence factor = 1.516. $(n_0, n_1, n_2, n_3) = (6,7,0,1)$.

(#14)

Marshall's $m_b = 4.370[\pm 0.020] + 0.869[\pm 0.017] \log(W)$ at Degelen with σ 0.076 and 95% confidence factor 1.494. $(n_0, n_1, n_2, n_3) = (9,46,0,15)$.

It remains to examine the second claim we made earlier, namely that the m_b values computed with Geotech's GLM method are better than those computed with other methods. We have separately regressed Marshall's (1988) and our m_b on the announced yields of the high-coupling shots detonated at NTS, using the same maximum-likelihood regression scheme. The results in Table 4 clearly indicate that for each event in common, our predicted yield is systematically closer to the announced yield than that based on Marshall's m_b values. About half of Geotech's NTS events in common with Nuttli's have the announced yields closer to the predictions based on our formula derived with Nuttli's $m_b(L_g)$, in accordance with Nuttli's claim that $m_b(L_g)$ could provide yield estimates as good as those based on the "good" m_b .

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Table 4. Comparison of NTS Yield Estimates							
Date	Event Code	Announced W		Estimated W			
		[KT]	$m_b(L_g)$	m _b (Marshall)	$m_b(P_{\text{max}}, \text{TG})$		
621005	MISSISSIPPI	110	87.8				
630913	BILBY	235	205.8		171.5		
631026	SHOAL	12.2	12.0		14.4		
641105	HANDCAR	12	7.3	7.5	10.7		
660224	REX	16	16.0	8.3	13.7		
660414	DURYEA	65	53.0	28.0			
660506	CHARTREUSE	70	72.6	44.6	56.5		
660527	DISCUSTHROWER	21	14.5	11.9			
660602	PILEDRIVER	56	93.5	113.9	93.7		
660630	HALFBEAK	300	351.9	412.1			
661220	GREELEY	825	727.2	644.9			
670520	COMMODORE	250	175.7	229.3			
670523	SCOTCH	150	199.4	131.5	146		
670526	KNICKERBOCKER	71	70.4	51.5			
680426	BOXCAR	1200	1096	825	1293		
681219	BENHAM	1100	1205	899	1122		
691029	CALABASH	110	106.1	113.0			
700526b	FLASK	105	99.6	98.9			
701217	CARPETBAG	220	240.9	183.3			
701218	BANEBERRY	10	12.8	21.9			
710708	MINIATA	80	124.2	82.4			
730426	STARWORT	85	96.5	100.0			
	# of Events	·····	22+14+1+30	19+13+1+27	9+2+1+2		
	$\hat{\sigma}_{MLE}(m_b)$		0.086	0.186	0.091		
	2σ Factor		1.717	2.799	1.630		

 $[\]hat{W}(m_b(L_g))$ estimated with the formula #8.

 $[\]hat{W}(m_b, Marshall)$ estimated with the formula #7.

 $[\]hat{W}(m_b,TG)$ estimated with the formula #1.

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Patton (1988) repeated Nuttli's (1986a) procedure to estimate the yields of 69 NTS high-coupling shots recorded at LLNL's high-quality digital network. Based on his regression result, the predicted $m_b(L_g)$ at explosive yields of 10, 50, 100, 150KT are 5.159, 5.687, 5.914, and 6.047, respectively. Nuttli's (1986a) original regression with 22 NTS shots recorded at WWSSN stations gave 5.072, 5.607, 5.837, and 5.972, respectively (cf. formula *5 in Table 2). Our formula (#8), which is based on Nuttli's (1986a) $m_b(L_g)$ measurements exclusively, gives 5.132, 5.642, 5.861, and 5.990 at 10, 50, 100, and 150KT, respectively. It is obvious that our maximum-likelihood scheme gives $m_b(L_g)$ estimates closer to Patton's results at all levels of explosive yield. In other words, including the censored information in the regression as proposed in this study does improve the determination of the calibration curve, regardless of what type of magnitude is used.

1.4 DISCUSSION AND CONCLUSIONS

Officially announced yields of underground nuclear explosions are often truncated or incomplete. In this study, we have presented a maximum-likelihood regression scheme which takes all the censored yields into account to refine the estimated m_b :yield relationship with an attempt to make the maximum use of the available data. Preliminary applications of this scheme to events from several test sites of different geology show that it is indeed a superior procedure, as compared to the conventional least-squares approach. The same algorithm can be applied to other magnitude measurements such as M_S , $m_b(L_g)$ or RMS L_g values etc.

Nuttli's L_g work (1986a, 1986b) proposed that careful analysis of L_g peak amplitude data from explosions could produce yield estimates nearly as accurate as the best teleseismic estimates. Based on the assumption that his $m_b(L_g)$:yield formulae are site independent, he obtained a m_b bias estimate (relative to NTS) of 0.35 and 0.54 at Shagan River and Degelen Mountain, respectively. The combination of these two values would seem to be consistent with our preliminary m_b bias estimates of 0.40 (10KT) and 0.435 (100KT) based on events from Eastern Kazakhstan including Shagan River and Degelen Mountain.

Our regression with Marshall's (1987) m_b values suggests that there is a m_b bias of 0.112 and 0.150 at Konystan and Degelen, respectively, relative to Shagan River for 100KT shots. At 150KT, the bias becomes 0.117 and 0.173, respectively. Marshall's m_b values generally have better quality than the ISC (International Seismological Centre, Newbury, U.K.) bulletin data which Nuttli (1987) used. Thus combining this m_b (Marshall) bias estimate with Nuttli's m_b - $m_b(L_g)$ offset, 0.23, would imply that there is a $m_b(L_g)$ bias of approximately 0.23 - 0.15 = 0.08 and 0.23 - 0.173 = 0.057 at 100KT and 150KT, respectively, between Shagan River and Degelen Mountain. Linear finite-difference calculations by Jih and McLaughlin (1988) and Jih *et al.* (1989) also suggest that there should be observable coupling variations

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affecting L_g amplitude. We are currently expanding Geotech's m_b database to investigate such spatial variation among three subregions of Eastern Kazakhstan (Jih *et al.*, 1990a; 1990b). At any rate, our preliminary analysis using Nuttli's $m_b(L_g)$ values tends to suggest that the regionalized calibration curves should provide a better result. For instance, formulae (#8) and (#9) would give a better fit than the formula (*5) in Table 2 for NTS events. In principle, this should be true not just for $m_b(L_g)$ alone. Porting any empirical magnitude: yield calibration curve from one site to another could be unreliable in some cases. The difference between formula (#10) for Shagan River and formula (#14) for Degelen Mountain is an example.

Recent theoretical studies on L_g (Lilwall, 1988; Jih *et al.*, 1989; Frankel, 1989) seem to agree that in a medium where the velocity increases with depth a smaller and smaller focal sphere of pS will be trapped as depth increases, thus decreasing the L_g amplitude. Since the larger shots are buried more deeply, this would imply that in general the slope in $m_b(L_g)$: yield relationship would be less than that in the m_b : yield relationship, as indicated in formulae (#1) through (#9).

Special purpose magnitudes, like m_Q in Marshall *et al.* (1979) which include corrections for source depth and source region attenuation should be, in principle, superior to m_b for estimating the explosive yield. However, the present study has shown that this may not be the case (*cf.* Table 2). The success of the pP and t^* corrections depends on the accuracy of the corrections. In our examples, the network m_b (or, m_2 in Marshall *et al.*, 1979), which were only corrected for the instrument gain, geometrical spreading (Veith and Clawson, 1972) as well as the station terms, would give fairly good yield estimates. Finally, the results in Table 2 seem to indicate that the phase "b" (*i.e.*, the first peak to the first trough) of the teleseismic P wave could give the yield estimate equally well as does the phase "max". However, further investigation is necessary.

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SECTION II

MAGNITUDE: YIELD RELATIONSHIP AT VARIOUS TEST SITES

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II.1 SUMMARY

We have conducted a systematic analysis of the magnitude:yield relationship at several test sites using miscellaneous magnitudes. The main tool of this study is a linear-regression scheme "MLE-CY" (Jih *et al.*, 1990a; 1990b) which takes all censored yields (*e.g.*, yield < 20 KT or 100 KT < yield < 150 KT) into account to refine the determination of the calibration curve. The majority of the recently published 96 Soviet explosive yields (Bocharov *et al.*, 1989; Vergino, 1989) and the U.S. announced yields (Springer and Kinaman, 1971, 1975) were heavily truncated or rounded, and hence the maximum-likelihood approach would seem ideal to make full use of the yield information. The regression routine we use is very similar to the maximum-likelihood estimator used in computing the optimal network m_b values based on the censored station amplitude measurements due to clipping and to noise (Blandford and Shumway, 1982; Jih and Shumway, 1989). In the non-censored case, it gives results identical to those derived by the standard least squares, corresponding to the two extreme cases of Ericsson's (1971) curve-fitting method which puts different variances in both the independent and the dependent variables.

In the following sections, we will tabulate the maximum-likelihood m_b :yield calibration curves which symbolically correspond to $\sigma(m_b)/\sigma(Y)=0$ and ∞ , respectively. Several noteworthy results are summarized here:

Including the censored yields in the regression does improve the accuracy of the estimates (cf. Tables 2C and 2D). In reality, both the magnitude and the yield measurements are subject to error. Pending the determination as to which of the two extreme hypotheses, namely $\sigma(m_b)/\sigma(Y)=0$ and $\sigma(m_b)/\sigma(Y)=\infty$, is closer to the real situation, we also included the results based on Ericsson's method with various $\sigma(m_b)/\sigma(Y)$. As expected, we can see the smooth transition of estimated parameters (i.e., the slope and the intercept) as $\sigma(m_b)/\sigma(Y)$ varies (cf. Tables 2A, 4A, 5C, 6C, and 7B). Thus the censored cases with nontrivial $\sigma(m_b)/\sigma(Y)$ values could be "interpolated". Our maximum-likelihood regression scheme and Ericsson's method represent two different directions in

m,-Yield Calibration Curves

- extending the standard least squares. In the future, Efron's bootstrap (Efron, 1979; Efron and Tibshirani, 1985) or other resampling techniques could be incorporated into Ericsson's curve-fitting routine to estimate the confidence interval.
- [2] For Shagan events, Ringdal's $RMS L_g$ provides the smallest scatter around the calibration curve, provided that low-yield events with $m_b(RMS L_g) < 5.5$ or yield < 40KT (e.g. the explosion on 10 Feb 72) are excluded. Geotech's GLM method (Blandford and Shumway, 1982) gives network m_b values better than almost all other magnitudes based on teleseismic P waves and $\log(\Psi_{\infty})$, in terms of both the yield estimation (cf. Tables 2B and 5C) and the m_b scaling against Ringdal's $RMS L_g$ (cf. Tables 5F and 9A). For all five test sites we have compared, m_b measurements reported by ISC and NEIS are biased high systematically at low yields (cf. Tables 2C, 4D, 5E, and 5D).
- [3] A direct estimation of the test site bias (cf. Tables 9A and 9B) suggests that Nuttli's (1987, 1988) Degelen puzzle could be invalid simply because of the relatively poorer quality m_b (ISC) used. Our data indicate that the Shagan River Test Site is more efficient in exciting teleseismic P waves than Degelen Mountain, consistent with our previous modeling study (Jih and McLaughlin, 1988). Also, the test site bias is yield dependent, in agreement with other observational study.
- [4] We present an alternative approach to derive the m_b adjustment converting cratering shots to contained explosions of the same yield (cf. Tables 8A and 8B). The correction derived by this approach seems to match that by the multichannel deconvolution method (Der et al., 1985) rather well.
- [5] Degelen Mountain is the only test site that has a decreasing $\log(P_{\text{max}}/P_{\text{a}})$ and $\log(P_{\text{b}}/P_{\text{a}})$ with increasing yields (cf. Tables 6D, 8A, and 8B). It is also the only test site for which the phase "a" (i.e., zero-crossing to first peak) shows the smallest scatter around the calibration curve, as compared to the phases "b" (i.e., first peak to first trough) and "max" (i.e., max peak-to-trough or trough-to-peak in the first 5 seconds). Both the mountainous topography (which causes complex pP interference) as well as the testing practice (e.g., the relatively shallow and abnormal shot depths) could be responsible. At Shagan River, the phase "b" has the smallest scatter around the calibration curve (cf. Tables 5C and 5D). These observations confirm the conjecture (DARPA, 1981) that in a proper environment the first cycle could give better results than does "max" phase.
- [6] The scale depth for Konystan explosions is 146±1 meters, and the depth of burial [DOB] is roughly proportional to the quartic root of the yield, rather than the cubic root as frequently cited at NTS (cf. Table 7B). This empirical scaling rule is applicable to Shagan River test site, but not Degelen Mountain. For Konystan and Shagan regions, the yields estimated using depth scaling have accuracy comparable to those using m_b.

m_b-Yield Calibration Curves

II.2 NTS

	Table 2A. m _b :Yield Relation of NTS High-Coupling Shots									
(Earlier Studie	(Earlier Studies)									
# of Events ¹	Magnitude	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	σ(<i>m_b</i>)	2σ Factor ²	Method			
22+0+0+0	Nuttli (1986a)	?	0.765±0.027	4.307±0.067			LS			
69+0+0+0	Patton (1988)	00	0.755±0.022	4.404±0.048	0.098	1.818	LS			
(This Study)										
# of Events	Magnitude	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2σ Factor	Method			
22+14+1+30	Nuttli, $m_b(L_g)$	0	0.761±0.033	4.336±0.193	0.116	2.019	MLE-CY			
22+14+1+30	Nuttli, $m_b(L_g)$	∞	0.730±0.018	4.402±0.038	0.086	1.717	MLE-CY			
19+13+1+29	ISC	0	0.787±0.067	4.006±0.379	0.190	3.036	MLE-CY			
19+13+1+29	ISC	00	0.693±0.035	4.199±0.074	0.136	2.475	MLE-CY			
19+13+1+27	Marshall	0	0.982±0.062	3.581±0.351	0.210	2.672	MLE-CY			
19+13+1+27	Marshall	8	0.833±0.049	3.892±0.105	0.186	2.799	MLE-CY			
9+2+1+2	TG, P _a	0	0.893±0.088	3.165±0.450	0.204	2.863	MLE-CY			
9+2+1+2	TG, P _a	00	0.835±0.065	3.283±0.147	0.175	2.632	MLE-CY			
9+2+1+2	TG, P _b	0	0.887±0.052	3.441±0.279	0.124	1.901	MLE-CY			
9+2+1+2	TG, P _b	∞	0.866±0.040	3.484±0.089	0.108	1.775	MLE-CY			
9+2+1+2	TG, P _{max}	0	0.872±0.045	3.716±0.253	0.105	1.744	MLE-CY			
9+2+1+2	TG, P _{max}	∞	0.857±0.034	3.747±0.075	0.091	1.630	MLE-CY			
22+0+0+0	Nuttli, $m_b(L_g)$	0	0.760±0.040	4.340±0.232	0.082	1.646	LS			
22+0+0+0	Nuttli, $m_b(L_g)$	0.1	0.759±	4.342±			Eriasson			
22+0+0+0	Nuttli, $m_b(L_g)$	1	0.745±	4.370±			Ericsson			
22+0+0+0	Nuttli, $m_b(L_g)$	5	0.737±	4.385±			Ericsson			
22+0+0+0	Nuttli, $m_b(L_g)$	100	0.737±	4.386±			Ericsson			
22+0+0+0	Nuttli, $m_b(L_g)$	00	0.737±0.029	4.386±0.060	0.081	1.659	LS			

^{1) #} of "exact" yields, # of left-censored yields, # of right-censored yields, and # of bounded yields.

²⁾ the multiplicative uncertainty factor in the yield [KT] at 95% confidence level.

m_b-Yield Calibration Curves

Table 2A. m _b :Yield Relation of NTS High-Coupling Shots (Continued)									
(This Studies)								
# of Events	Magnitude	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2σ Factor	Method		
9+0+0+0	TG, P _{max}	0	0.870±0.052	3.719±0.284	0.098	1.684	LS		
9+0+0+0	TG, P _{max}	0.1	0.869±	3.720±			Ericsson		
9+0+0+0	TG, P _{max}	1	0.860±	3.738±			Ericsson		
9+0+0+0	TG, P _{max}	5	0.854±	3.750±			Ericsson		
9+0+0+0	TG, P _{max}	100	0.854±	3.751±			Ericsson		
9+0+0+0	TG, P _{max}	000	0.854±0.044	3.751±0.093	0.097	1.692	LS		

For purposes of estimating explosion yields, the media are divided into three types: unsaturated material, e.g., alluvium and dry tuff; water-saturated rock; and granite. The U.S. granite shots PILEDRIVER and SHOAL will be discussed in the next section again.

If we ignore the different corner frequencies between events of large and small yields, and put all high-coupling shots in one single regression, then both Geotech's $m_b(P_{\rm max})$'s and Marshall's m_b give a slope matching Murphy's (1977) theoretical prediction, 0.85, rather well (cf. Table 2A).

At NTS, yields estimated from m_b alone have a random uncertainty factor of 1.45 at the 95% confidence (i.e., 2σ) level, provided the best "official" m_b values are used (U.S. Congress/OTA, 1988). None of the magnitudes listed in Table 2A reaches such a precision. However, it is also clear that the m_b based on our $P_{\rm max}$ is relatively more precise than other unclassified m_b measurements. The phase "a" has much larger variance than the phase "max" at NTS, possibly because of the small amplitudes measured were near the noise.

m_b-Yield Calibration Curves

	Table 2B. Maximum-Likelihood Yield Estimates of NTS Shots							
Date	Event Code	Announced W		Estimated W				
		[KT]	$m_b(L_g)$	m _b (Marshall)	$m_b(P_{\text{max}}, TG)$			
621005	MISSISSIPPI	110	87.8					
630913	BILBY	235	205.8		171.5			
631026	SHOAL	12.2	12.0		14.4			
641105	HANDCAR	12	7.3	7.5	10.7			
660224	REX	16	16.0	8.3	13.7			
660414	DURYEA	65	53.0	28.0				
660506	CHARTREUSE	70	72.6	44.6	56.5			
660527	DISCUSTHROWER	21	14.5	11.9				
660602	PILEDRIVER	56	93.5	113.9	93.7			
660630	HALFBEAK	300	351.9	412.1				
661220	GREELEY	825	727.2	644.9				
670520	COMMODORE	250	175.7	229.3				
670523	SCOTCH	150	199.4	131.5	146			
670526	KNICKERBOCKER	71	70.4	51.5	_			
680426	BOXCAR	1200	1096	825	1293			
681219	BENHAM	1100	1205	899	1122			
691029	CALABASH	110	106.1	113.0				
700526b	FLASK	105	99.6	98.9				
701217	CARPETBAG	220	240.9	183.3				
701218	BANEBERRY	10	12.8	21.9				
710708	MINIATA	80	124.2	82.4				
730426	STARWORT	85	96.5	100.0				
	# of Events		22+14+1+30	19+13+1+27	9+2+1+2			
	ô _{MLE} (m _b)		0.086	0.186	0.091			
	2σ Factor		1.717	2.799	1.630			
	ρ˙		0.990	0.942	0.994			

 $[\]mbox{\ensuremath{^{\bullet}}}\ \rho\mbox{:}$ the correlation coefficient between the magnitudes and the log yields.

m_h-Yield Calibration Curves

For each event in common with Marshall's in Table 2B, the yield predicted with Geotech's $m_b(P_{\rm max})$ is always closer to the announced value than that based on Marshall's m_b values. As noted in Jih *et al.* (1990a), this would strongly suggest that Geotech's m_b values have smaller systematic error, since the same regression methodology was used.

Patton (1988) utilized Nuttli's procedure to estimate the yields for 69 high-coupling shots at NTS. The NTS explosions Patton used were clustered around $m_b(L_g) \approx 5.8$. Beyond that level, the difference in yield estimates between Nuttli's and Patton's predictions are by no means negligible. For $m_b(L_g) = 6.0$, they predict the yield to be 163KT (N) and 130KT (P), respectively. At $m_b(L_g) = 6.5$, the predictions are 736KT (N) and 597KT (P), respectively.

Since Patton (1988) did not release the individual yields or $m_b(L_g)$ in his paper, we need an alternative approach to make the comparison. The data recorded at LLNL's regional digital network have quality better than those WWSSN film chips which Nuttli (1986a) read. It would seem reasonable to assume that the m_b predicted by Patton's regression is more accurate than Nuttli's. Table 2c below indicates that regressing Nuttli's $m_b(L_g)$ measurements against the censored yields with our maximum-likelihood scheme gives m_b estimates very close to Patton's results at all levels of explosive yield. In other words, including the censored information in the regression as proposed in Jih *et al.* (1990a, 1990b) does improve the determination of the calibration curves, regardless of what magnitude is used.

m_k-Yield Calibration Curves

Table 2C. Expected magnitudes of NTS High-Coupling Explosions										
	(Regressing the magnitudes on the yields)									
(Earlier Studies)										
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT					
Nuttli ¹	22+0+0+0	5.072	5.607	5.837	5.972					
Patton ²	69+0+0+0	5.159	5.687	5.914	6.047					
(This Study)										
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT					
Nuttli ³	22+0+0+0	5.123	5.638	5.860	5.989					
Nuttli ⁴	22+14+1+30	5.132	5.642	5.861	5.990					
ISC	19+13+1+26	4.892	5.376	5.585	5.707					
Marshall	19+13+1+27	4.725	5.307	5.558	5.704					
TG, Pa	9+2+1+2	4.118	4.701	4.953	5.100					
TG, <i>P_b</i>	9+2+1+2	4.350	4.955	5.216	5.368					
TG, P _{max}	9+2+1+2	4.604	5.202	5.460	5.610					

- 1) Nuttli (1986a): $m_b(L_q) = 4.307[\pm 0.067] + 0.765[\pm 0.027]\log(W)$ for $5.2 < m_b(L_q) < 6.7$.
- 2) Patton (1988): $m_b(L_g) \approx 4.404[\pm 0.048] + 0.755[\pm 0.022]\log(W)$ for $4.22 < m_b(L_g) < 6.7$.
- 3) Nuttli's $m_b(L_g)$ values regressed with the least square, $\sigma(m_b)/\sigma(Y) = \infty$ (cf. Table 2A).
- 4) Nuttli's $m_b(L_g)$ values regressed with MLE-CY, $\sigma(m_b)/\sigma(Y) = \infty$ (cf. Table 2A).

Table 2C raises a question as how to evaluate different calibration curves. Apparently the trade off between α and β should be taken into account. Judging on the slope, β , alone could be very misleading. For instance, in comparison with the 2 slopes which we obtained with Nuttli's $m_b(L_g)$ measurements, his original slope is closer to that of Patton's (*cf.* Table 2A), and yet our formulae actually predict the yields as well as the magnitudes closer to those of Patton's (Tables 2C and 2D).

m_h-Yield Calibration Curves

Table	Table 2D. Expected Yields [KT] of NTS High-Coupling Explosions									
(Earlier Studies)	(Earlier Studies)									
m _b :Y Curve	$m_b(L_g) = 4.5$	$m_b(L_g) = 5.0$	$m_b(L_g) = 5.5$	$m_b(L_g) = 6.0$						
Nuttli ¹	1.8	8.1	36.3	163.3						
Patton ²	1.3	6.2	28.3	130.0						
(This Study)	(This Study)									
m _b :Y Curve	$m_b(L_g) = 4.5$	$m_b(L_g) = 5.0$	$m_b(L_g) = 5.5$	$m_b(L_g) = 6.0$						
Nuttli ³	1.4	6.8	32.5	155.1						
Nuttli ⁴	1.4	6.6	32.0	154.9						
m _b :Y Curve	m _b =4.5	m _b =5.0	<i>m_b</i> =5.5	$m_b = 6.0$						
Marshall	5.4	21.4	85.2	339.5						
TG, P _{max}	7.6	29.0	111.3	426.4						

- 1) Nuttli (1986a): $m_b(L_g) = 4.307[\pm 0.067] + 0.765[\pm 0.027]\log(W)$ for $5.2 < m_b(L_g) < 6.7$.
- 2) Patton (1988): $m_b(L_g) = 4.404[\pm 0.048] + 0.755[\pm 0.022]\log(W)$ for $4.22 < m_b(L_g) < 6.7$.
- 3) Nuttli's $m_b(L_g)$ values regressed with the least square (cf. Table 2A).
- 4) Nuttli's $m_b(L_g)$ values regressed with MLE-CY (cf. Table 2A).

Due to the different yield relationships for teleseismic P and L_g at NTS, the yield estimates at the same "magnitude" level are very different. We will compare the $m_b(P)$ - $m_b(L_g)$ offset of various test sites in a later section (cf. Table 9A).

In comparing with Nuttli's regression results, we noticed that his original formula (Equation 1 in Table 2C) seems not reproducible. His data set (cf. Nuttli, 1986a, page 2144) included the Pahute Mesa event HANDLEY which had a bounded yield of >1000KT. However, Nuttli seemed to have treated the yield as exactly 1000KT in his calculations (cf. Figures 7 and 9 of Nuttli, 1986a). Different symbols for the 2 granite events PILEDRIVER and SHOAL were used in his figures (cf. Nuttli, 1986a, pages 2145 and 2147). Also, Nuttli imposed a $m_b(L_g)$ range of applicability (from 5.2 to 6.7) on his calibration curve.

We have tested eight possible combinations with Nuttli's $m_b(L_g)$ measurements:

- · including NTS granite events or not,
- limiting $m_b(L_a)$ to [5.2,6.7] or not,
- assuming HANDLEY was 1000KT or deleting HANDLEY from the regression.

None of the eight extra experiments could give an "exactly identical" formula to that given by Nuttli (1986a), even if the computer's "machine ε " is accounted for. It seems very likely that Nuttli was using the "Y-regression" models, i.e., $\sigma(m_b)/\sigma(Y) \approx 0$, with some unspecified constraint on the data set. However, for all cases we have tested, the comparisons of MLE results (using Nuttli's data) against Patton's result confirmed consistently that including the censored data would improve the regression.

II.3 U.S. AND FRENCH SAHARA SHOTS IN GRANITE

Т	able 3A. m_b :	Yield Re	elation of French	Sahara and N	TS Events	s in Granite	,
# of Events	m _b	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2σ Factor	Method
4+0+0+0	TG, P _a	0	0.875±0.056	3.365±0.270	0.035	1.203	LS
4+0+0+0	TG, P _a	∞	0.869±0.049	3.374±0.083	0.035	1.203	LS
4+0+0+0	TG, P _b	0	1.048±0.064	3.334±0.325	0.048	1.234	LS
4+0+0+0	TG, <i>P</i> _b	∞	1.040±0.066	3.348±0.113	0.048	1.235	LS
4+0+0+0	TG, P _{max}	0	1.011±0.058	3.657±0.310	0.042	1.211	LS
4+0+0+0	TG, P _{max}	∞	1.004±0.058	3.668±0.099	0.042	1.212	LS
4+4+1+0	TG, P _a	0	0.928±0.044	3.258±0.195	0.061	1.353	MLE-CY
4+4+1+0	TG, Pa	∞	0.905±0.036	3.296±0.048	0.056	1.328	MLE-CY
4+6+1+0	TG, P _b	0	1.049±0.020	3.334±0.092	0.035	1.169	MLE-CY
4+6+1+0	TG, <i>P</i> _b	00	1.040±0.022	3.348±0.028	0.037	1.178	MLE-CY
4+6+1+0	TG, P _{max}	0	1.014±0.018	3.658±0.084	0.032	1.154	MLE-CY
4+6+1+0	TG, P _{max}	∞	1.008±0.018	3.659±0.022	0.032	1.157	MLE-CY

^{*) 2} NTS events in granite and 9 French Sahara explosions; no P_a for EMERAUDE and TURQUOISE.

m_b-Yield Calibration Curves

	Table 3B	. Yield Estima	ates of Frenc	ch & U.S. Sh	ots in Gran	nite	
Event	Official W	$m_b(P_{\rm max})$	LS	MLE	$m_b(P_b)$	LS	MLE
	[KT]		[KT]	[KT]		[KT]	[KT]
BERYL	>20.0	4.986	20.6	20.8	4.779	23.8	23.8
CORUNDON	<20.0	4.214	3.5	3.6	3.900	3.4	3.4
EMERAUDE	<20.0	4.569	7.9	8.0	4.263	7.6	7.6
GRENAT	<20.0	4.766	12.4	12.6	4.497	12.7	12.7
OPALE	<20.0	3.894	1.7	1.7	3.853	3.1	3.1
RUBIS	52.0	5.432	57.2	57.5	5.170	56.4	56.5
SAPHIR	120.0	5.720	110.7	111.1	5.468	109.2	109.2
TOURMALINE	<20.0	4.646	9.4	9.5	4.429	10.9	11.0
TURQUOISE	<20.0	4.223	3.6	3.6	3.942	3.7	3.7
SHOAL	12.2	4.739	11.7	11.8	4.455	11.6	11.6
PILEDRIVER	56.0	5.436	57.7	58.0	5.195	59.7	59.7
#	of Events		4+0+0+0	4+6+1+0		4+0+0+0	4+6+1+0
($\mathfrak{I}_{MLE}(m_b)$		0.042	0.032		0.048	0.037
2	2σ Factor		1.212	1.157		1.235	1.178
	ρ		0.997	0.999		0.996	0.999

Table 3C. Expected m_b of U.S. and French Shots in Granite									
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT				
TG, P _a	4+4+1+0	4.201	4.833	5.106	5.265				
TG, P _b	4+6+1+0	4.388	5.115	5.428	5.611				
TG, P _{max}	4+6+1+0	4.668	5.372	5.675	5.853				

II.4 EASTERN KAZAKHSTAN AREA

	Table 4A		eld Calibration (Curve at Easter	n Kazakh	stan	
# of Events	m _b	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2σ Factor	Metriod
19+55+0+17	ISC	0	0.715±0.029	4.532±0.156	0.105	1.972	MLE-CY
19+55+0+17	ISC	∞	0.687±0.014	4.570±0.018	0.076	1.660	MLE-CY
19+55+0+17	NEIS	0	0.745±0.039	4.607±0.213	0.157	2.639	MLE-CY
19+55+0+17	NEIS	- 00	0.655±0.019	4.725±0.023	0.113	2.222	MLE-CY
19+55+0+17	Sykes	0	0.717±0.024	4.535±0.129	0.088	1.755	MLE-CY
19+55+0+17	Sykes	∞	0.696±0.012	4.563±0.015	0.063	1.520	MLE-CY
19+0+0+0	Marshall	0	0.823±0.050	4.419±0.279	0.098	1.728	LS
19+0+0+0	Marshall	0.1	0.822±	4.420±			Ericsson
19+0+0+0	Marshall	1	0.802±	4.448±			Ericsson
19+0+0+0	Marshall	5	0.791±	4.466±			Ericsson
19+0+0+0	Marshall	œ	0.789±0.039	4.466±0.060	0.096	1.748	LS
19+55+0+17	Marshall	0	0.798±0.025	4.462±0.133	0.109	1.872	MLE-CY
19+55+0+17	Marshall	00	0.759±0.015	4.516±0.018	0.087	1.696	MLE-CY
12+3+0+5	TG, Pa	0	0.951±0.042	3.497±0.208	0.094	1.577	MLE-CY
12+3+0+5	TG, P _a	00	0.926±0.037	3.537±0.059	0.088	1.552	MLE-CY
13+3+0+5	TG, P _b	0	0.951±0.042	3.795±0.220	0.096	1.594	MLE-CY
13+3+0+5	TG, P _b	8	0.924±0.037	3.837±0.059	0.091	1.571	MLE-CY
13+3+0+5	TG, P _{max}	0	0.921±0.047	4.064±0.257	0.102	1.666	MLE-CY
13+3+0+5	TG, P _{max}	∞	0.892±0.039	4.110±0.062	0.093	1.617	MLE-04

^{*)} including Shagan River (Balapan), Konystan (Murzhik), and Degelen Mountain.

In Table 4A, we regressed all Eastern Kazakh explosions with announced yields (Bocharov $et\ al.$, 1989) against various m_b values of Marshall (1987), ISC, NEIS, and ours. Detailed descriptions of the explosions are listed in later sections according to the subregion they belong to.

m_b-Yield Calibration Curves

	Table 4B. L	east-Squares	Yield Estimat	es of E. Kaza	kh Shots	
Event, Region	Official W	ISC	NEIS	Sykes	Marshall	TG, P _{max}
	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]
651121, D	29.0	32.0	48.0	31.0	27.7	25.6
660213, D	125.0	159.6	188.5	155.8	185.1	159.0
660320, D	100.0	115.7	188.5	112.8	98.6	88.2
660507, D	4.0	2.4	1.6	2.3	2.2	2.8
670922, M	10.0	8.8	8.7	8.5	7.6	
680929, D	60.0	60.8	48.0	59.1	58.5	50.1
690723, D	16.0	16.8	17.2	16.2	20.6	15.6
691130, S	125.0	115.7	95.2	97.2	100.9	121.2
691228, M	40.0	44.1	34.1	42.8	47.7	
710425, D	90.0	83.9	67.6	92.9	109.5	69.5
710606, M	16.0	23.2	17.2	21.0	22.0	
711009, M	12.0	12.2	12.2	12.5	14.0	
711021, M	23.0	23.2	24.3	23.1	25.8	
720210, S	16.0	16.8	17.2	14.7	14.0	22.1
720328, D	6.0	6.4	6.2	7.0	8.0	9.2
720816, D	8.0	4.6	6.2	6.8	6.4	7.6
720902, M	2.0	3.4	4.4	3.0	2.6	
721102, S	165.0	159.6	188.5	202.4	168.6	207.6
721210, S	140.0	115.7	95.2	108.8	86.7	133.4
# of Eve	ents	19+0+0+0	19+0+0+0	19+0+0+0	19+0+0+0	13+0+0+0
ô _{MLE} (<i>n</i>	1 _b)	0.080	0.120	0.070	0.096	0.097
2σ Fac	tor	1.669	2.278	1.570	1.748	1.638
ρ		0.983	0.957	0.987	0.980	0.984

D = Degelen, S = Shagan (Balapan), M = Murzhik (Konystan).

m_b-Yield Calibration Curves

	Table 4C.	Maximum-Likeli	hood Yield Estir	nates of E. Kaza	akh Shots	
Event, Region	Official W	ISC	NEIS	Sykes	Marshall	TG, P _{max}
	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]
651121, D	29.0	31.7	43.9	30.8	27.3	25.4
660213, D	125.0	169.5	179.1	160.8	196.8	162.9
660320, D	100.0	121.2	179.1	115.5	102.1	89.5
660507, D	4.0	2.2	1.3	2.2	1.9	2.7
670922, M	10.0	8.3	7.6	8.2	7.1	
680929, D	60.0	62.0	43.9	59.6	59.3	50.4
690723, D	16.0	16.2	15.3	15.9	20.1	15.4
691130, S	125.0	121.2	88.6	99.2	104.7	123.6
691228, M	40.0	44.3	30.9	42.9	48.0	
710425, D	90.0	86.7	62.4	94.8	113.9	70.2
710606, M	16.0	22.7	15.3	20.7	21.5	
711009, M	12.0	1,1.6	10.7	12.2	13.4	
711021, M	23.0	22.7	21.7	22.9	25.3	
720210, S	16.0	16.2	15.3	14.4	13.4	21.9
720328, D	6.0	5.9	5.3	6.7	7.4	9.0
720816, D	8.0	4.2	5.3	6.5	6.0	7.4
720902, M	2.0	3.0	3.7	2.8	2.3	
721102, S	165.0	169.5	179.1	210.2	178.5	213.6
721210, S	140.0	121.2	88.6	111.4	89.4	136.4
# of Eve	ents	19+55+0+17	19+55+0+17	19+55+0+17	19+55+0+17	13+3+0+5
ô _{MLE} (n	n _b)	0.076	0.113	0.063	0.087	0.093
2o Fac	ctor	1.660	2.222	1.520	1.696	1.617
ρ		0.993	0.985	0.996	0.994	0.988

D = Degelen, S = Shagan (Balapan), M = Murzhik (Konystan).

m_b-Yield Calibration Curves

	Table 4D. Expected r	n_b of Eastern	Kazakhstan Ex	plosions	
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT
ISC	19+55+0+17	5.256	5.736	5.943	6.064
NEIS	19+55+0+17	5.380	5.837	6.034	6.150
Sykes	19+55+0+17	5.260	5.747	5.956	6.079
Marshall	19+55+0+17	5.274	5.805	6.033	6.167
TG, Pa	12+3+0+5	4.462	5.109	5.388	5.551
TG, P _b	13+3+0+5	4.761	5.407	5.685	5.848
TG, P _{max}	13+3+5+4	5.003	5.626	5.895	6.052

II.5 SHAGAN RIVER TEST SITE

ı a	ble 5A. Nuclear E	explosions at Sna	agan Hiver (Bai	apan) Region	
Date	Lat	Long	Depth	Yield	Rock
	[N]	(E)	[m]	[KT]	
650115	49.9350	79.0094	178	100-150	Sa
680619	49.9803	78.9855	316	<20	Sa
691130	49.9243	78.9558	472	125	Co
710630	49.9460	78.9805	217	<20	Co
720210	50.0243	78.8781	295	16	Al
721102	49.9270	78.8173	521	165	Al
721210	50.0270	78.9956	478	140	TS

Sa = Sandstone, Al = Aleurolite (Siltstone),

Co = Conglomerate, TS = Tuffaceous Sandstone

[from Bocharov et al. (1989) and Vergino (1989)]

m_b-Yield Calibration Curves

	Table 5B. Reported m_b of Shagan River Explosions											
Date	ISC	NEIS	Sykes	Marshall	Stewart	Stewart	Stewart					
	m _b	m_b	m _b	m _b	m _b	log(Ψ _∞)	Mo					
650115	5.8	6.3	5.905	5.931	5.96	3.87	15.80					
680619	5.4	5.5	5.350	5.354	5.60	3.31	15.24					
691130	6.0	6.0	5.954	6.048	6.14	4.00	15.93					
710630	5.2	5.4	5.290	5.027	5.29	2.98	14.91					
720210	5.4	5.5	5.370	5.370	5.58	3.22	15.15					
721102	6.1	6.2	6.181	6.224	6.39	4.38	16.31					
721210	6.0	6.0	5.989	5.996	6.06	4.38	16.31					

^{*)} Averaged over EKA, YKA, GBA, and WRA.

Т	able 5B. R	eported m _b	of Shagan Riv	er Explosions	s (Continued))
Date	EKA	Nuttli	Ringdal	TG	TG	TG
	m _b	$m_b(L_g)$	RMS Lg	$m_b(P_a)$	$m_b(P_b)$	$m_b(P_{\text{max}})$
650115	5.98	5.87	5.950°	5.495	5.734	5.882
680619	5.70			4.620	5.002	5.263
691130	6.30		6.043	5.380	5.770	5.977
710630	5.34			4.472	4.768	5.041
720210	5.58	5.55	5.4**	4.805	5.074	5.306
721102	6.41	6.04	6.118	5.592	5.940	6.189
721210	6.08	6.09	6.095		5.786	6.015
710425***	N/A	N/A	5.862	N/A	N/A	N/A

^{*)} Inferred indirectly from Nuttli's $m_b(L_g) = 5.87$ (Ringdal and Marshall, 1989).

^{**)} Low SNR for L_g phase (see text).

^{***)} A Degelen event used in Ringdal (1989).

m_b-Yield Calibration Curves

	Table 5C. Mag	gnitude:	Yield Calibration	n Curve at Shaga	ın River A	\rea	
# of Events	Magnitude	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2 _o Factor	Method
4+2+0+1	ISC	0	0.655±0.132	4.584±0.753	0.116	2.267	MLE-CY
4+2+0+1	ISC	∞	0.628±0.055	4.645±0.097	0.077	1.753	MLE-CY
4+2+0+1	NEIS	0	0.722±0.709	4.621±1.225	0.189	3.346	MLE-CY
4+2+0+1	NEIS	000	0.614±0.093	4.807±0.131	0.131	2.671	MLE-CY
4+2+0+1	Sykes	0	0.720±0.105	4.481±0.600	0.095	1.833	MLE-CY
4+2+0+1	Sykes	00	0.698±0.054	4.525±0.096	0.069	1.577	MLE-CY
4+0+0+0	Marshall	0	0.795±0.137	4.385±0.811	0.088	1.669	LS
4+0+0+0	Marshall	0.1	0.795±	4.387±			Ericsson
4+0+0+0	Marshall	1	0.777±	4.420±			Ericsson
4+0+0+0	Marshall	5	0.767±	4.439±			Ericsson
4+0+0+0	Marshall	∞	0.767±0.105	4.441±0.206	0.087	1.685	LS
4+2+0+1	Marshall	0	0.768±0.089	4.421±0.510	0.098	1.803	MLE-CY
4+2+0+1	Marshall	00	0.741±0.052	4.476±0.090	0.076	1.606	MLE-CY
4+2+0+1	EKA, m _b	0	0.705±0.246	4.724±1.457	0.236	4.654	MLE-CY
4+2+0+1	EKA, m _b	∞	0.568±0.104	4.983±0.181	0.165	3.809	MLE-CY
4+2+0+1	Stewart, m _b	0	0.667±0.220	4.738±1.293	0.207	4.170	MLE-CY
4+2+0+1	Stewart, m _b	∞	0.570±0.087	4.926±0.152	0.138	3.044	MLE-CY
4+2+0+1	Stewart, log(Ψ∞)	0	1.098±0.124	1.865±0.467	0.172	2.061	MLE-CY
4+2+0+1	Stewart, log(Ψ∞)	oo .	0.953±0.135	2.134±0.237	0.189	2.498	MLE-CY
4+2+0+1	Stewart, Mo	0	1.099±0.124	13.795±1.942	0.172	2.061	MLE-CY
4+2+0+1	Stewart, Mo	00	0.953±0.135	14.064±0.237	0.189	2.497	MLE-CY
3+0+0+1	Nuttli, $m_b(L_g)$	0	0.587±0.346	4.742±2.035	0.160	3.516	MLE-CY
3+0+0+1	Nuttli, $m_b(L_g)$	00	0.546±0.106	4.835±0.207	0.087	2.085	MLE-CY
4 +0+0+1	Ringdal, RMS L _g	0	1.075±0.123	3.768±0.741	0.026	1.119	MLE-CY
4 +0+0+1	Ringdal, RMS L _g	000	1.025±0.134	3.873±0.281	0.027	1.130	MLE-CY

^{*)} Degelen event 710425 was used instead of Shagan event 720210.

m_k-Yield Calibration Curves

Ta	Table 5C. Magnitude: Yield Calibration Curve at Shagan River Area (Continued)										
# of Events	Magnitude	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	σ(<i>m_b</i>)	2σ Factor	Method				
3+2+0+1	TG, Pa	0	0.759±0.075	3.873±0.382	0.082	1.640	MLE-CY				
3+2+0+1	TG, P _a	00	0.738±0.041	3.910±0.069	0.060	1.456	MLE-CY				
4+2+0+1	TG, P _b	0	0.812±0.044	4.083±0.238	0.051	1.332	MLE-CY				
4+2+0+1	TG, P _b	00	0.803±0.028	4.101±0.050	0.041	1.264	MLE-CY				
4+2+0+1	TG, P _{max}	0	0.811±0.074	4.298±0.422	0.082	1.593	MLE-CY				
4+2+0+1	TG, P _{max}	000	0.788±0.039	4.336±0.068	0.067	1.475	MLE-CY				

 m_b (NEIS) are biased high at low yields for Shagan explosions simply because NEIS averages the signals reported. Consequently their m_b vs. log(W) slope is underestimated, which in turn causes the yields of the high-yield explosions to be overestimated. The yields estimated by Geotech's P_b seem to have accuracy at least as good as that based on P_{max} .

In Tables 5B and 5C, Stewart's m_b , $\log(\Psi_\infty)$, and M_o are those which are averaged over four arrays: Eskdalemuir (EKA) Scotland, Yellowknife (YKA) Canada, Gauribidanur (GBA) India, and Warramunga (WRA) Australia. The scatter is slightly reduced as compared to that based on a single array EKA. Marshall's m_b values are based on the ISC bulletin recordings (Marshall, personal communication).

Apparently the RMS L_g averaged over the bandpassed multi-channel signals recorded at NORSAR fit the announced yields very well. However, more data may be needed to further quantify its performance (Ringdal and Hansen, 1989) (cf. Table 5D). If Shagan event 720210 (which had poor L_g SNR at NORSAR) is included, the results would show a slightly greater scatter ($\sigma = 0.056$ and 0.040 for cases 0 and ∞ , respectively). In Tables 5C through 5E, we have excluded this event at Ringdal's suggestion (Ringdal, personal communication).

Zavadil and Eisenhauer conjectured that the first or "b" phase could replace the phase "max." However, these AFTAC researchers and many others did not find convincing evidence to support their argument (DARPA, 1981). It seems this conjecture could well be valid at least for Shagan River. Among the three phases we measured, the phase "b" has the smallest scatter (cf. Table 5C), and it gives the best yield estimates (cf. Table 5D). At NTS and Sahara, the phase "b" has precision much better than the phase "a". At Degelen Mountain, phase "a" shows the smallest scatter, possibly because phases "b" and "max" are severely contaminated by the scattering at the free-surface topography (cf. Table 6C).

m_b-Yield Calibration Curves

Table 5	D. Maxim	num-Likeli	hood Yiel	d Estimates	of Shagan Exp	olosions	
Date & Official W	ISC	NEIS	Sykes	Marshall	Stewart m _b	log(Ψ _∞)	M _o
[KT]	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]
650115, 100-150	69.2	269.6	94.9	92.0	65.0	66.3	66.4
680619, <20	16.0	13.4	15.2	15.3	15.2	17.1	17.1
691130, 125	144.2	87.6	111.6	132.4	134.5	90.8	90.8
710630, <20	7.7	9.2	12.5	5.5	4.3	7.7	7.7
720210, 16	16.0	13.4	16.5	16.1	14.0	13.8	13.8
721102, 165	208.1	185.3	235.9	226.0	369.2	227.6	227.6
721210, 140	144.2	87.6	125.2	112.7	97.4	227.6	227.6
ô _{MLE} (m _b)	0.077	0.131	0.069	0.076	0.138	0.189	0.189
2σ Factor	1.753	2.671	1.577	1.606	3.044	2.498	2.497
ρ	0.986	0.958	0.989	0.991	0.957	0.962	0.963

Table 5D.	Maximum-L	ikelihood Yi	ield Estimate	s of Shagan Ex	plosions (C	ontinued)	
Date & Official W	EKA	Nuttli*	Nuttli	Ringdal***	P_a	P _b	P _{max}
[KT]	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]
650115, 100-150	56.9	109	78.8	106.3	140.6	108.2	89.3
680619, <20	18.3				9.2	13.3	14.6
691130, 125	208.5			131.0	98.2	119.9	117.8
710630, <20	4.2				5.8	6.8	7.6
720210, 16	11.2	42	16.5		16.3	16.3	16.6
721102, 165	325.8	183	161.5	155.0	190.3	195.3	218.9
721210, 140	85.4	212	199.4	147.2		125.6	131.7
$\delta_{MLE}(m_b)$	0.165		0.087	0.027	0.060	0.041	0.067
2σ Factor	3.809		2.085	1.130	1.456	1.264	1.475
ρ	0.939		0.965	0.979	0.996	0.998	0.994

^{*)} Nuttli (1986b): $m_b(L_g) = 4.307[\pm 0.067] + 0.765[\pm 0.027]\log(W)$ for $5.2 < m_b(L_g) < 6.7$.

^{**)} Nuttli's $m_b(L_g)$ regressed by our maximum-likelihood code.

^{***)} Degelen event 710425 was used instead of Shagan event 720210.

In 1988 the United States and the Soviet Union signed a bilateral agreement whereby each country was permitted to monitor at close distance an underground nuclear explosion at the other's main test site. The Soviet JVE (Joint Verification Experiment) shot was detonated on September 14, 1988, near the southern edge of the Shagan River Test Site. The New York Times states that the American and Soviet on-site measurements are said to give yields of 115KT and 122KT, respectively, for the Soviet JVE explosions (Sykes and Ekstrom, 1989). NORSAR's $RMS L_g$ measurement for this event was 5.969 (Ringdal and Marshall, 1989). Assuming that the actual yield was between 100 and 150KT, as suggested by P. G. Richards, the regression using NORSAR's $RMS L_g$ data including this event would give an estimate of 111.2KT, which is very close to Sykes' 113KT based on the average of m_b and M_S (Sykes and Ekstrom, 1989). The $\sigma(m_b)$ and the 95% factor in yield associated with NORSAR's data reduce from 0.027 and 1.130 (cf. Table 5D) to 0.026 and 1.122, respectively.

Table	Table 5E. Expected Magnitudes of Shagan Explosions									
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT					
ISC	4+2+0+1	5.273	5.711	5.900	6.011					
NEIS	4+2+0+1	5.421	5.850	6.035	6.144					
Sykes	4+2+0+1	5.223	5.711	5.921	6.044					
Marshall	4+2+0+1	5.217	5.735	5.958	6.088					
EKA, m _b	4+2+0+1	5.551	5.948	6.119	6.219					
Stewart, m _b	4+2+0+1	5.496	5.895	6.067	6.167					
Stewart, log(Ψ _∞)	4+2+0+1	3.087	3.753	4.040	4.208					
Stewart, Mo	4+2+0+1	15.017	15.683	15.970	16.138					
Nuttli, $m_b(L_g)$	3+0+0+1	5.381	5.762	5.926	6.023					
Ringdal, RMS L _g	4+0+0+1		5.614	5.923	6.103					
TG, P _a	3+2+0+1	4.648	5.164	5.386	5.516					
TG, P _b	4+2+0+1	4.904	5.465	5.707	5.848					
TG, P _{max}	4+2+0+1	5.133	5.684	5.922	6.062					

In Table 5D, we have listed two sets of yield estimates based on Nuttli's (1986b) $m_b(L_g)$ measurements. Although Nuttli's $m_b(L_g)$ database for Shagan had only four events in common with that of Bocharov, it is clear that regressing the $m_b(L_g)$ (or m_b) on each test site

separately, whenever the data are available, would give better results than the global calibration curve as recommended by Nuttli.

Table 5E indicates that our $m_b(P_{\rm max})$ matches Ringdal's $RMS L_g$ very well (except at low yields). Note that $m_b(L_g)$ is defined to be equal to m_b in eastern North America, which has geology similar to Eastern Kazakhstan. Thus relative to $m_b(L_g)$ scaling, our $m_b(P_{\rm max})$ seem to have the smallest bias, as compared to other m_b . We have also regressed various magnitudes on Ringdal's $RMS L_g$ with slope fixed at 1 (Table 5F). As expected, our $m_b(P_b)$ and $m_b(P_{\rm max})$ possess the strongest correlation, the smallest scatter around the fitted straight line, as well as the smallest standard error in the estimated intercept.

Table 5F. Various Magni	tudes Versus Ringdal	's $RMS L_g$ for Shagan Ever	nts
Magnitude	σ(<i>m_b</i>)	Intercept	ρ
ISC	0.068	-0.034±0.028	0.968
NEIS	0.143	0.066±0.058	0.840
Sykes	0.094	0.002±0.039	0.960
Marshall	0.112	0.030±0.050	0.926
EKA, m _b	0.136	0.149±0.068	0.907
Stewart, m _b	0.125	0.105±0.062	0.912
Stewart, log(Ψ _∞)	0.211	-1.951±0.106	0.955
Stewart, Mo	0.211	9.979±0.106	0.955
Nuttli, $m_b(L_g)$	0.085	-0.016±0.049	0.986
TG, P _a	0.077	-0.560±0.039	0.968
TG, P _b	0.058	-0.266±0.026	0.988
TG, P _{max}	0.064	-0.057±0.029	0.982

^{*)} Regressed on $RMS L_g$ with slope 1 and free intercept.

It should not be surprising that M_o and $\log(\Psi_{\infty})$ reported by the four British arrays give identical slope, σ , ρ , and yield estimates *etc*. (Tables 5C, 5D, and 5F) since Stewart (1988) computed the seismic moment, M_o , as

$$M_o \equiv 4 \pi d V_o^2 \Psi_\infty$$

where d = 2.4 g/cc and $V_p = 5.0$ km/sec are the presumed density and the P-wave velocity of the source material.

II.6 DEGELEN MOUNTAIN

Table 6A. Nuclear Explosions at Degelen Mountainous Region									
Date	Lat	Long	Depth	Yield	Rock				
	[N]	(E)	[m]	[KT]					
611011	49.77272	77.99500	116	<20	Gr				
620202	49.77747	78.00164	238	<20	Gr				
640315	49.81597	78.07517	220	20-150	Gr				
640516	49.80772	78.10197	253	20-150	Gr				
640719	49.80908	78.09292	168	<20	Gr				
641116	49.80872	78.13344	194	20-150	QP				
650303	49.82472	78.05267	196	<20	Gr				
650511	49.77022	77.99428	103	<20	Gr				
650617	49.82836	78.06686	152	<20	Gr				
650729	49.77972	77.99808	126	<20	Gr				
650917	49.81158	78.14669	156	<20	QP				
651008	49.82592	78.11144	204	<20	QP				
651121	49.81919	78.06358	278	29	Gr				
651224	49.80450	78.10667	213	<20	QP				
660213	49.80894	78.12100	297	125	QP				
660320	49.76164	78.02389	294	100	QP				
660421	49.80967	78.10003	178	<20	Gr				
660507	49.74286	78.10497	274	4	QP				
660629	49.83442	78.07336	187	20-150	Gr				
660721	49.73667	78.09703	170	<20	QP				

Gr = Granite, QP = Quartz Porphyrite, Po = Porphyrite, QS = Quartz Syenite [from Bocharov et al. (1989)]

m_b-Yield Calibration Curves

Table (6A. Nuclear Explos	ions at Degelen Mo	ountainous Reg	ion (Continued)	
Date	Lat	Long	Depth	Yield	Rock
	[N]	(E)	[m]	[KT]	
660805	49.76431	78.04242	171	<20	Gr
660819	49.82708	78.10875	134	<20	QP
660907	49.82883	78.06375	117	<20	Gr
661019	49.74711	78.02053	185	20-150	Gr
661203	49.74689	78.03336	153	<20	Gr
670130	49.76744	77.99139	131	<20	QS
670226	49.74569	78.08231	241	20-150	QP
670325	49.75361	78.06300	152	<20	Gr
670420	49.74161	78.10542	225	20-150	QP
670528	49.75642	78.01689	262	<20	QP
670629	49.81669	78.04903	195	<20	Gr
670715	49.83592	78.11817	161	<20	QP
670804	49.76028	78.05550	160	<20	Gr
671017	49.78089	78.00383	181	20-150	Gr
671030	49.79436	78.00786	173	<20	Gr
671208	49.81714	78.16378	150	<20	QP
680107	49.75442	78.03094	237	<20	Gr
680424	49.84519	78.10322	127	<20	QP
680611	49.79300	78.14508	149	<20	QP
680712	49.75469	78.08994	172	<20	Gr
680820	49.82264	78.07447	208	<20	Gr
680905	49.74161	78.07558	162	<20	Gr
680929	49.81197	78.12194	290	60	QP
681109	49.80053	78.13911	125	<20	QP
681218	49.74594	78.09203	194	<20	Gr
690307	49.82147	78.06267	214	20-150	Gr

Gr = Granite, QP = Quartz Porphyrite, Po = Porphyrite, QS = Quartz Syenite [from Bocharov *et al.* (1989) and Vergino (1989)]

m_b-Yield Calibration Curves

l able (6A. Nuclear Explos	ions at Degelen M	ountainous Reg	ion (Continued)	1
Date	Lot	Long	Depth	Yield	Roc
	[N]	[E]	[m]	[KT]	
690516	49.75942	78.07578	184	<20	Gr
690704	49.74603	78.11133	219	<20	QP
690723	49.81564	78.12961	175	16	QP
690911	49.77631	77.99669	190	<20	Gr
691001	49.78250	78.09831	144	<20	Gr
691229	49.73367	78.10225	86	<20	QF
700129	49.79558	78.12389	214	20-150	Po
700327	49.74781	77.99897	138	<20	Gr
700527	49.73131	78.09861	66	<20	QF
700628	49.80150	78.10681	332	20-150	Gı
700724	49.80972	78.12839	154	<20	QF
700906	49.75975	78.00539	212	<20	G
701217	49.74564	78.09917	193	<20	G
710322	49.79847	78.10897	283	20-150	G
710425	49.76853	78.03392	296	90	G
710525	49.80164	78.13883	132	<20	G
711129	49.74342	78.07850	203	<20	Gı
711215	49.82639	77.99731	115	<20	G
711230	49.76003	78.03714	249	20-150	Gi
720310	49.74531	78.11969	171	<20	QF
720328	49.73306	78.07569	124	6	QF
720607	49.82675	78.11547	208	20-150	QF
720706	49.73750	78.11006	81	<20	QF
720816	49.76547	78.05883	139	8	G
721210	49.81939	78.05822	264	20-150	G
721228	49.73919	78.10625	132	<20	QF
	• • • • • • • • • • • • • • • • • • • 		+		

Gr = Granite, QP = Quartz Porphyrite, Po = Porphyrite, QS = Quartz Syenite [from Bocharov *et al.* (1989) and Vergino (1989)]

m_b-Yield Calibration Curves

	7	able 6B. F	Reported m_b	of Degelen M	lountain Expl	osions	
Date	ISC	NEIS	Sykes	Marshall	TG, P _a	TG, P _b	TG, P _{max}
	m _b	m _b	m _b				
611011							
620202							
640315	5.6	5.6	5.600	5.563			
640516	5.6	5.6	5.600	5.549			
640719	5.4	5.5	5.400	5.433			
641116	5.6	6.0		5.642			
650303	5.5	5.6	5.500	5.443			
650511	4.9	5.2	4.900	4.742			
650617	5.2	5.4	5.200	5.244			
650729	4.5	4.5	4.500				_
650917	5.2	5.6	5.200	5.219			
651008	5.4	5.7	5.400	5.471			
651121	5.6	5.8	5.600	5.605	4.877	5.154	5.364
651224	5.0	5.0	5.000	4.944			
660213	6.1	6.2	6.100	6.256	5.642	5.892	6.084
660320	6.0	6.2	6.000	6.040	5.337	5.626	5.852
660421	5.3	5.4	5.300	5.370			
660507	4.8	4.8	4.800	4.734	3.994	4.235	4.488
660629	5.6	5.6	5.600	5.508			
660721	5.3	5.4	5.300	5.360			
660805	5.4	5.5	5.400	5.390			
660819	5.1	4.8	5.100	4.633			
660907	4.8	4.7	4.800	4.661			
661019	5.6	5.7	5.600	5.669			
661203	4.8	4.8	4.800	4.600			
670130	4.8	4.8	4.800	4.627			
670226	6.0	6.0	6.000	6.034	5.355	5.599	5.823
670325	5.3	5.3	5.300	5.320			

m_b-Yield Calibration Curves

	Table 6	B. Reported	d m _b of Deg	jelen Mountain	Explosions	(Continued)	
Date	ISC	NEIS	Sykes	Marshall	TG, Pa	TG, P _b	TG, P _{max}
	m _b	m _b	m _b	m _b	m _b	m _b	m _b
670420	5.5	5.7	5.500	5.556			
670528	5.4	5.4	5.400	5.464			
670629	5.3	5.3	5.300	5.336			
670715	5.4	5.4	5.400	5.387			
670804	5.3	5.3	5.300	5.316			
671017	5.6	5.7	5.600	5.629			
671030	5.3	5.5	5.300	5.413			
671208	5.4	5.4	5.400	5.314			
680107	5.1	5.3	5.100	4.977			
680424	5.0	5.0	5.000	4.911			
680611	5.2	5.3	5.200	5.240			
680712	5.3	5.4	5.300	5.169			
680820	4.8	4.8	4.800	4.761			
680905	5.4	5.5	5.400	5.439			
680929	5.8	5.8	5.800	5.861	5.127	5.434	5.629
681109	4.9	4.9	4.900	4.751			
681218	5.0	5.2	5.000	5.044			
690307	5.6	5.5	5.600	5.664			
690516	5.2	5.3	5.200	5.264			
690704	5.2	5.3	5.200	5.241			
690723	5.4	5.5	5.400	5.504	4.596	4.922	5.169
690911	5.0	5.0	5.000	4.910	3.977	4.236	4.578
691001	5.2	5.3	5.200	5.256			
691229	5.1	4.6	5.100	4.217			
700129	5.5	5.6	5.500	5.599			
700327	5.0	5.2	5.000	4.929			
700527	3.8		3.800				
700628	5.7	5.9	5.700	5.870			

m_b-Yield Calibration Curves

	Table 6	B. Reported	$d m_b$ of Deg	elen Mountair	Explosions ((Continued)	
Date	ISC	NEIS	Sykes	Marshall	TG, P _a	TG, P _b	TG, P _{max}
	m _b	m _b	m _b				
700724	5.3	5.3	5.300	5.337			
700906	5.4	5.6	5.400	5.533			
701217	5.4	5.5	5.400	5.433			
710322	5.7	5.8	5.700	5.767			
710425	5.9	5.9	5.940	6.076	5.301	5.568	5.758
710525	5.1	5.2	5.020	5.048			
711129	5.4	5.5	5.440	5.462		 -	
711215	4.9	4.9	4.900	4.677			
711230	5.7	5.8	5.780	5.838	4.984	5.349	5.526
720310	5.4	5.5	5.410	5.453			
720328	5.1	5.2	5.140	5.177	4.353	4.728	4.961
720607	5.4	5.5	5.400	5.422			
720706	4.4	4.4	4.420	4.275			
720816	5.0	5.2	5.130	5.105	4.339	4.622	4.887
721210	5.6	5.7	5.600	5.715	4.977	5.355	5.534
721228			4.900				

Table 6B indicates that for Degelen events, all other m_b 's are systematically larger than ours by a Δm_b of approximately 0.2 to 0.3. The m_b offset is less significant for Shagan events (cf. Tables 6B and 5E), however. This is possibly due to the different focusing and defocusing patterns between Shagan-Europe and Degelen-Europe paths. In our WWSSN database, there were 8 and 10 European stations which detected the Shagan event 650115 (100-150KT) and Degelen event 710425 (90KT), respectively. The averaged m_b residuals of the European WWSSN stations for these two events are 0.07 ± 0.133 and 0.122 ± 0.057 , respectively. Marshall's database has a heavy clustering of ISC stations in Europe, and hence the resulting m_b offset may just be reflecting the even more severe path focusing effects enhanced by the ISC clustering in the western Europe.

	Table 6	SC. m _b :	Yield Calibration	Curve at Dege	len Mour	ntain	
# of Events	m _b	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	$\sigma(m_b)$	2σ Factor	Method
9+46+0+15	ISC	0	0.833±0.022	4.362±0.114	0.069	1.466	MLE-CY
9+46+0+15	ISC	00	0.809±0.015	4.392±0.018	0.058	1.392	MLE-CY
9+46+0+15	NEIS	0	0.861±0.036	4.445±0.195	0.129	1.997	MLE-CY
9+46+0+15	NEIS	∞	0.773±0.024	4.556±0.028	0.110	1.920	MLE-CY
9+46+C+15	Sykes	0	0.803±0.019	4.414±0.102	0.062	1.426	MLE-CY
9+46+0+15	Sykes	00	0.786±0.012	4.438±0.015	0.051	1.345	MLE-CY
9+0+0+0	Marshall	0	0.912±0.067	4.300±0.377	0.097	1.635	LS
9+0+0+0	Marshall	0.1	0.912±	4.300±			Ericsson
9+0+0+0	Marshall	1	0.897±	4.322±			Ericsson
9+0+0+0	Marshall	5	0.885±	4.338±			Ericsson
9+0+0+0	Marshall	100	0.884±	4.340±			Ericsson
9+0+0+0	Marshall	∞	0.884±0.059	4.340±0.090	0.096	1.647	LS
9+46+0+15	Marshall	0	0.908±0.022	4.318±0.115	0.083	1.525	MLE-CY
9+46+0+15	Marshall	00	0.869±0.017	4.370±0.020	0.076	1.494	MLE-CY
9+1+0+3	TG, Pa	0	0.981±0.048	3.449±0.226	0.087	1.505	MLE-CY
S+1+0+3	TG, P _a	∞	0.959±0.044	3.479±0.066	0.084	1.499	MLE-CY
9+1+0+3	TG, P _b	0	0.972±0.058	3.752±0.297	0.108	1.665	MLE-CY
9+1+0+3	TG, P _b	00	0.939±0.052	3.798±0.079	0.103	1.654	MLE-CY
9+1+0+3	TG, P _{max}	0	0.931±0.062	4.033±0.333	0.108	1.709	MLE-CY
9+1+0+3	TG, P _{max}	000	0.899±0.051	4.079±0.078	0.099	1.660	MLE-CY

m_b-Yield Calibration Curves

	Table 6D. Exp	pected m _b of D	egelen Explos	ions	
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT
ISC	9+46+0+15	5.201	5.767	6.010	6.153
NEIS	9+46+0+15	5.329	5.870	6.103	6.239
Sykes	9+46+0+15	5.223	5.772	6.009	6.147
Marshall	9+46+0+15	5.239	5.846	6.108	6.261
TG, P _a	9+1+0+2	4.438	5.108	5.397	5.566
TG, P _b	9+1+0+2	4.737	5.393	5.676	5.841
TG, P _{max}	9+1+0+2	4.978	5.606	5.876	6.034

II.7 KONYSTAN (MURZHIK) AREA

	Table 7A. Explosions at Konystan (Murzhik) Region								
Date	Lat	Long	Depth	Yield	Rock	ISC	NEIS	Sykes	Marshall
	[N]	[E]	[m]	[KT]		m _b	m _b	m _b	m _b
651014	49.9906	77.6357	048	1.1	Al				
661218	49.9246	77.7472	427	20-150	Po	5.8	5.9	5.800	5.922
670916	49.9372	77.7281	230	<20	Sa	5.3	5.3	5.300	5.245
670922	49.9596	77.6911	229	10	Al	5.2	5.3	5.200	5.160
671122	49.9419	77.6868	227	<20	Al	4.8		4.800	4.410
681021	49.7279	78.4863	31	0.2	Ar				
681112	49.7124	78.4613	31	0.2x3	Gs				
690531	49.9503	77.6942	258	<20	Al	5.3	5.4	5.300	5.290
691228	49.9373	77.7142	388	46	Al	5.7	5.7	5.700	5.791
700721	49.9524	77.6729	225	<20	Sa	5.4	5.4	5.400	5.376
701104	49.9892	77.7624	249	<20	Ро	5.4	5.4	5.400	5.439
710606	49.9754	77.6603	299	16	Al	5.5	5.5	5.480	5.526
710619	49.9690	77.6408	290	<20	Ро	5.4	5.5	5.410	5.538
711009	49.9779	77.6414	237	12	Al	5.3	5.4	5.320	5.371
711021	49.9738	77.5973	324	23	Sa	5.5	5.6	5.510	5.580
720826	49.9820	77.7166	285	<20	Al	5.3	5.5	5.370	5.363
720902	49.9594	77.6409	185	2	Sa	4.9	5.1	4.880	4.788

Sa = Sandstone, AI = Aleurolite (Siltstone), Po = Porphyrite, Gs = Gritstone [from Bocharov *et al.* (1989) and Vergino (1989)]

m_b-Yield Calibration Curves

	Table 7B. m _b :Yield Calibration Curve at Konystan Area							
# of Events	m _b	$\frac{\sigma(m_b)}{\sigma(Y)}$	Slope	Intercept	σ(m _b)	2σ Factor	Method	
6+7+0+1	ISC	0	0.632±0.097	4.659±0.518	0.093	1.962	MLE-CY	
6+7+0+1	ISC	00	0.602±0.036	4.691±0.042	0.057	1.542	MLE-CY	
6+7+0+1	NEIS	0	0.500±0.106	4.894±0.573	0.099	2.490	MLE-CY	
6+7+0+1	NEIS	000	0.472±0.023	4.920±0.027	0.046	1.562	MLE-CY	
6+7+0+1	Sykes	0	0.638±0.080	4.650±0.426	0.077	1.740	MLE-CY	
6+7+0+1	Sykes	o e	0.617±0.031	4.671±0.036	0.048	1.429	MLE-CY	
6+0+0+0	Marshall	0	0.791±0.102	4.498±0.547	0.081	1.598	LS	
6+0+0+0	Marshall	0.1	0.790±	4.498±			Ericsson	
6+0+0+0	Marshall	1	0.772±	4.519±			Ericsson	
6+0+0+0	Marshall	5	0.761±	4.531±			Ericsson	
6+0+0+0	Marshall	100	0.760±	4.532±			Ericsson	
6+0+0+0	Marshall	∞	0.760±0.077	4.532±0.091	0.079	1.613	LS	
6+7+0+1	Marshall	0	0.806±0.065	4.495±0.347	0.089	1.666	MLE-CY	
6+7+0+1	Marshall	00	0.768±0.039	4.535±0.045	0.069	1.516	MLE-CY	
6+7+0+1	DOB*	0	0.278±0.400	2.136±0.972	0.143	10.713	MLE-CY	
6+7+0+1	DOB	00	0.245±0.024	2.164±0.028	0.035	1.915	MLE-CY	

^{*)} Depth of Burial.

Our maximum-likelihood regression routine can be applied to estimate the depth scaling rule as well (Jih, 1990). The result in Table 7B indicates that the scale depth for Konystan explosions is 146 ± 1 meters. Furthermore, The depth of burial [DOB] is proportional to the quartic root of the yield, rather than the cubic root as frequently cited at NTS (e.g., Evernden and Marsh, 1987). For Konystan test site, the yields estimated using DOB seem to have accuracy comparable to m_b (Table 7C). This is not the case for Degelen region, however (Jih. 1990).

m_b-Yield Calibration Curves

Table	Table 7C. Maximum-Likelihood Yield Estimates of Konystan Explosions							
Date	Official W	ISC	NEIS	Sykes	Marshall	DOB		
	[KT]	[KT]	[KT]	[KT]	[KT]	[KT]		
661218	20-150	69.5	118.8	67.4	64.2	80.1		
670916	<20	10.3	6.4	10.4	8.4	6.4		
670922	10	7.0	6.4	7.2	6.5	6.3		
671122	<20	1.5	0.6	1.6	0.7	6.1		
690531	<20	10.3	10.4	10.4	9.6	10.2		
691228	46	47.4	44.8	46.4	43.3	54.2		
700721	<20	15.0	10.4	15.2	12.5	5.8		
701104	<20	15.0	10.4	15.2	15.1	8.8		
710606	16	22.1	16.9	20.4	19.6	18.7		
710619	<20	15.0	16.9	15.7	20.3	16.5		
711009	12	10.3	10.4	11.2	12.3	7.2		
711021	23	22.1	27.5	22.8	23.0	25.9		
720826	<20	10.3	16.9	13.6	12.0	15.4		
720902	2.0	2.2	2.4	2.2	2.1	2.6		
$\hat{\sigma}_{MLE}(m_b)$ or $\hat{\sigma}$	MLE(DOB)	0.057	0.046	0.048	0.069	0.035		
2o Fac	tor	1.542	1.562	1.429	1.516	1.915		
ρ		0.990	0.993	0.993	0.992	0.971		

Table 7D. Expected m _b & DOB of Konystan Explosions								
m _b :Y Curve	# of Events	10KT	50KT	100KT	150KT			
ISC	6+7+0+1	5.293	5.714	5.895	6.001			
NEIS	6+7+0+1	5.392	5.723	5.865	5.948			
Sykes	6+7+0+1	5.289	5.720	5.906	6.014			
Marshall	6+7+0+1	5.302	5.839	6.070	6.205			
DOB (meter)	6+7+0+1	257	380	451	498			

II.8 CRATERING VERSUS NON_CRATERING EXPLOSIONS

Tables 8A and 8B list the $\Delta_1 m_b \equiv \hat{m_b}(P_{\text{max}}) - \hat{m_b}(P_a)$ and $\Delta_2 m_b \equiv \hat{m_b}(P_b) - \hat{m_b}(P_a)$ at four different test sites. As the yield increases from 10KT to 150KT, the Δm_b decreases steadily, except at Degelen Mountain. This could be yet another indication that the D.O.B. at Degelen does not quite follow the depth scaling. Note that Sahara Test Site has the same trend as Shagan.

Table 8A. Expected $\hat{m_b}(P_{\text{max}})$ - $\hat{m_b}(P_a)$ At 4 Test Sites							
Test Site	10KT	50KT	100KT	150KT			
NTS	0.486	0.501	0.507	0.510			
Sahara	0.467	0.539	0.569	0.588			
KTS	0.541	0.517	0.507	0.501			
Shagan River	0.485	0.520	0.536	0.546			
Degelen	0.540	0.498	0.479	0.468			

Table 8B. Expected $\hat{m_b}(P_b)$ - $\hat{m_b}(P_a)$ At 4 Test Sites							
Test Site	10KT	50KT	100KT	150KT			
NTS	0.232	0.254	0.263	0.268			
Sahara	0.187	0.282	0.322	0.346			
KTS	0.299	0.298	0.297	0.297			
Shagan River	0.256	0.301	0.321	0.332			
Degelen	0.299	0.285	0.279	0.275			

McLaughlin et al. (1985) studied the ratio of the P_a phase and $P_{\rm max}$ phase of presumed Shagan River contained and cratering explosions by comparing the WWSSN station m_b 's. The motivation was that the logarithm of amplitude ratio of $P_{\rm max}/P_a$ of event 650115 was significantly smaller than other presumed contained explosions in the vicinity. Assuming the phase P_a is unaffected by the influence of the non-linear free-surface interference, then an adjustment to the $m_b(P_{\rm max})$ should be able to convert that to a contained explosion of the

same yield. McLaughlin et al. (1985) concluded that a correction between 0.17 and 0.27 is needed for this conversion, assuming a yield of 125KT.

Based on 46 Shagan River explosions recorded at EKA, Ringdal and Marshall (1989) derived a value of 0.75 as their mean $\log(P_{\text{max}}/P_a)$ across the EKA array using the same techniques as used in McLaughlin *et al.* (1985). The cratering event 650115 had $m_b(P_{\text{max}}) - m_b(P_a) = 0.62$ at EKA, and hence they apply a correction of 5.87 + 0.75 - 0.62 = 6.00 for a hypothetical contained explosion with equivalent yield. Both Ringdal and Marshall (1989) and McLaughlin *et al.* (1985) have the same methodological drawback in that they did not take the yields of those reference contained explosions into account, due to the lack of data at the time.

We utilize the statistics in Tables 8A and 8B to illustrate that the correction by Ringdal and Marshall (1989) might be slightly more accurate than that in McLaughlin *et al.* (1985). In Table 8A, we have $\hat{m_b}(P_{\text{max}}) - \hat{m_b}(P_a) = 0.536$ at 100KT, and 0.546 at 150KT. Since for event 650115 our $m_b(P_{\text{max}}, \text{TG}) - m_b(P_a, \text{TG}) = 0.387$ (Table 5B), this would imply an adjustment of 0.149 (100KT) and 0.159 (150KT), and a corrected m_b of about 6.031 (100KT) and 6.041 (150KT), respectively. Note that the adjusted m_b at 150KT, 6.041, is almost identical to the "expected $m_b(P_{\text{max}})$ " of 6.062 (*cf.* Table 5E). The corrected m_b at 100KT would match that of Ringdal's rather well if the standard error in the uncorrected $m_b(P_{\text{max}})$, 5.882±0.046, is taken into account.

Der et al. (1985) deconvolved four contained and the cratering Shagan events [650115] recorded at EKA, and then they convolved the Green's functions with an appropriate attenuation operator as well as the source-time function of various yields of interest. By comparing the phases P_a and P_{max} of the synthetics, they obtained a cratering-to-contained correction of 0.15, 0.15, and 0.18 at 60, 125, and 300KT, respectively. The match with our result is remarkably good. This approach would seem very attractive if the database can be expanded to events covering a wide range of yields (and hence depths) and then the method can be applied to events in the same yield range.

II.9 TEST SITE BIAS

Table 9A. Expected $\hat{m_b}(P)$ - $\hat{m_b}(L_g)$ at Various Test Sites							
(Earlier Studies*)							
Test Site	Description 10KT 50KT 100KT				150KT		
NTS	m_b (ISC) - Nuttli's $m_b(L_g)$	-0.31	-0.31	-0.31	-0.31		
Shagan River	m_b (ISC) - Nuttli's $m_b(L_g)$	0.04	0.04	0.04	0.04		
Degelen	$m_b(ISC)$ - Nuttli's $m_b(L_g)$	0.27	0.27	0.27	0.27		
Degelen	m_b (Sykes) - Nuttli's $m_b(L_g)$	0.23	0.23	0.23	0.23		
Novaya Zemlya	m_b (ISC) - Nuttli's $m_b(L_g)$	-0.11	-0.11	-0.11	-0.11		
(This Study)							
Test Site	Description	10KT	50KT	100KT	150KT		
NTS	m_b (Marshall) - Patton's $m_b(L_g)$	-0.434	-0.380	-0.356	-0.343		
NTS	$m_b(P_{max}, TG)$ - Patton's $m_b(L_g)$	-0.555	-0.485	-0.454	-0.437		
Shagan River	m_b (Marshall) - Ringdal's RMS L_g		0.121	0.035	-0.015		
Shagan River	$m_b(P_{\text{max}}, \text{TG})$ - Ringdal's RMS L_g		0.070	-0.001	-0.041		
Degelen	m_b (Marshall) - Ringdal's RMS L_g		0.232	0.185	0.158		
Degelen	$m_b(P_{\text{max}}, \text{TG})$ - Ringdal's RMS L_g		-0.008	-0.047	-0.069		

^{*)} Nuttli (1987, 1988).

At Degelen and Shagan, our results show that the $m_b(P)$ - $m_b(L_g)$ has a decreasing tendency with increasing yield, contrary to the increasing trend at NTS. Results based on Marshall's m_b are consistent with ours.

Table 9B. Expected Test Site Bias							
(Earlier Studies)							
Test Sites	Description	10KT	50KT	100KT	150KT		
Shagan - NTS	Nuttli (1987)	0.35	0.35	0.35	0.35		
Degelen - NTS	Nuttli (1987)	0.54	0.54	0.54	0.54		
Shagan - Degelen	Nuttli (1987)	-0.19	-0.19	-0.19	-0.19		
Novaya Zemlya - NTS	Nuttli (1987)	0.20	0.20	0.20	0.20		
(This Study)							
Test Sites	Description	10KT	50KT	100KT	150KT		
Ringdal's RMS L_g (Shagan) - m_b (P_{max}	, TG, Sahara)		0.243	0.253	0.251		
Ringdal's $RMS L_g$ (Shagan) - $m_b(L_g)$ (Patton, NTS)		-0.073	0.009	0.056		
KTS - NTS	m _b (Marshall)	0.549	0.498	0.475	0.463		
KTS - NTS	$m_b(P_a, TG)$	0.344	0.408	0.435	0.451		
KTS - NTS	$m_b(P_b, TG)$	0.411	0.452	0.469	0.480		
KTS - NTC	$m_b(P_{\text{max}}, TG)$	0.399	0.424	0.435	0.442		
Shagan - NTS	m _b (Marshall)	0.492	0.428	0.400	0.384		
Shagan - NTS	$m_b(P_a, TG)$	0.530	0.463	0.433	0.416		
Shagan - NTS	$m_b(P_b, TG)$	0.554	0.510	0.491	0.480		
Shagan - NTS	$m_b(P_{\text{max}}, \text{TG})$	0.529	0.482	0.462	0.452		
Degelen - NTS	m _b (Marshall)	0.514	0.539	0.550	0.557		
Degelen - NTS	$m_b(P_a, TG)$	0.320	0.407	0.444	0.466		
Degelen - NTS	$m_b(P_b, TG)$	0.387	0.438	0.460	0.473		
Degelen - NTS	$m_b(P_{\text{max}}, \text{TG})$	0.374	0.404	0.416	0.424		
Sahara - NTS	$m_b(P_a, TG)$	0.083	0.132	0.153	0.165		
Sahara - NTS	$m_b(P_b, TG)$	0.038	0.160	0.212	0.243		
Sahara - NTS	$m_b(P_{\text{max}}, \text{TG})$	0.063	0.168	0.214	0.240		
KTS - Sahara	$m_b(P_a, TG)$	0.261	0.276	0.282	0.286		
KTS - Sahara	$m_b(P_b, TG)$	0.373	0.292	0.257	0.237		
KTS - Sahara	$m_b(P_{\text{max}}, TG)$	0.335	0.254	0.220	0.199		

m_b-Yield Calibration Curves

	Table 9B. Expected Test Site Bias (Continued)						
(This Study)							
Test Sites	Description	10KT	50KT	100KT	150KT		
Shagan - Sahara	$m_b(P_a, TG)$	0.447	0.331	0.280	0.251		
Shagan - Sahara	$m_b(P_b, TG)$	0.516	0.350	0.279	0.237		
Shagan - Sahara	$m_b(P_{\text{max}}, \text{TG})$	0.465	0.312	0.247	0.209		
Degelen - Sahara	$m_b(P_a, TG)$	0.237	0.275	0.291	0.301		
Degelen - Sahara	$m_b(P_b, TG)$	0.349	0.278	0.248	0.230		
Degelen - Sahara	$m_b(P_{\text{max}}, TG)$	0.310	0.234	0.201	0.181		
Shagan - Degelen	m _b (ISC)	0.072	-0.056	-0.110	-0.142		
Shagan - Degelen	m _b (NEIS)	0.092	-0.020	-0.068	-0.095		
Shagan - Degelen	m _b (Sykes)	0.000	-0.061	-0.088	-0.103		
Shagan - Degelen	m _b (Marshall)	-0.022	-0.111	-0.150	-0.173		
Shagan - Degelen	$m_b(P_a, TG)$	0.210	0.056	-0.011	-0.050		
Shagan - Degelen	$m_b(P_b, TG)$	0.167	0.072	0.031	0.007		
Shagan - Degelen	$m_b(P_{\text{max}}, TG)$	0.155	0.078	0.046	0.028		
Konystan - Degelen	m _b (ISC)	0.092	-0.053	-0.115	-0.152		
Konystan - Degelen	m _b (NEIS)	0.063	-0.147	-0.238	-0.291		
Konystan - Degelen	m _b (Sykes)	0.066	-0.052	-0.103	-0.133		
Konystan - Degelen	m_b (Marshall)	0.063	-0.007	-0.038	-0.056		
Konystan - Shagan	m _b (ISC)	0.020	0.003	-0.005	-0.010		
Konystan - Shagan	m _b (NEIS)	-0.029	-0.127	-0.170	-0.196		
Konystan - Shagan	m _b (Sykes)	0.066	0.009	-0.015	-0.030		
Konystan - Shagan	m_b (Marshall)	0.085	0.104	0.112	0.117		

The m_b bias between Sahara and Degelen is interesting in that different phases exhibit opposite tendency of bias change with yields. The bias determined with phase "a" increases with yields, while that of phases "b" and "max" decrease.

Based on Geotech's m_b : yield calibration curves, Shagan River would have more efficient P-wave coupling than does Degelen River by an offset of about 0.155 m.u. (magnitude unit)

and 0.046 m.u. at 10KT and 100KT, respectively. This m_b bias can be explained by the profound topography at Degelen Mountain which could cause strong P-to-S conversion, as illustrated by the linear finite-difference calculations (Jih and McLaughlin, 1988). The bias value currently used by the U.S. government is intended to be the most appropriate value for yields near the 150KT threshold of the 1974 Threshold Test Ban Treaty (TTBT). Our results in Table 9B provide a direct clues of how different the bias could be at lower yields.

A brief review of earlier work on test site bias may be interesting. Based on the P-wave seismograms of three granite explosions (PILEDRIVER, Shagan 680619, and Shagan 710630) recorded at EKA, Douglas (1987) concluded that the Shagan-NTS bias is about 0.5. which is very close to what we got with phases P_b and P_{max} (Table 9B). Stewart (1988) predicted a bias of 0.37 at m_b =5.0 and of 0.32 at m_b =6.5, based on the m_b averaged across four arrays: Eskdalemuir (EKA) Scotland, Yellowknife (YKA) Canada, Gauribidanur (GBA) India, and Warramunga (WRA) Australia. His predicted bias is yield-dependent, and it has a decreasing trend with increasing yield, which is consistent with our maximum-likelihood results in Table 9B. This tendency should not be surprising. Large-yield explosions generate predominantly low-frequency signals and low-yield explosions are relatively richer in higher frequencies, so a relatively large amount of energy is removed by the attenuation from low yield tests, hence the bias is greater for such low yield explosions. Furthermore, the bias between two sites is made up of more than just the attenuation in the mantle beneath the test site. A difference in depth containment laws and up-hole velocities between the test sites can have an effect on the observed amplitudes and hence on the final value of bias (Marshall, personal communication). The bias between any two test sites should be a sum of these effects. Murphy and Tzeng (1982) estimated the bias by comparing signals recorded near NTS and Semipalatinsk from Aleutian Islands earthquakes. They estimated the bias as 0.24 magnitude unit. Priestley et al. (1987) used a similar approach, and they estimated the bias as 0.34. It should be noted, however, that all these earlier bias estimates were made before the publication of Bocharov et al. (1989) and Vergino (1989).

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APPENDIX

GEOTECH'S MAXIMUM-LIKELIHOOD NETWORK mb: GLM90A

Short-period WWSSN vertical recordings (SPZ) of body waves from 96 nuclear explosions detonated at the Semipalatinsk Test Site, Eastern Kazakhstan, USSR, are being measured and added to our database to determine the optimal network magnitudes using the maximum-likelihood estimator (MLE), which accounts for the effects of data censoring due to clipping and to noise. As of now, our WWSSN database has been expanded to 124 events (totaling 366 usable "a", "b", and "max" event phases) from a variety of test sites. Only the stations at teleseismic distance (20 to 95 degrees) were used in the network m_b determination. (Therefore, some of the m_b values might be slightly different from those in an earlier report TGAL-87-05.) The 8501 good signals, 5699 noise measurements, and 1088 clipped recordings yield a $\hat{\sigma}_{MLE}$ 0.320.

The 124 events in Table A1 are grouped by test sites. The three numbers under the column "# of signals" represent the number of signals, noise, and clips associated with the P_{max} phase of each event. Except for the U.S. and French Sahara explosions which have specific code names, all the remaining events are identified with the dates and abbreviated test site codes shown below:

azg Azgir, U.S.S.R.

pne "PNE", Urals, U.S.S.R.

mek Murzhik (Konystan), E. Kazakh, U.S.S.R.

dek Degelen Mountain, E. Kazakh, U.S.S.R.

sek Shagan River (Balapan), E. Kazakh, U.S.S.R.

nnz Northern Novaya Zemlya, U.S.S.R.

snz Southern Novaya Zemlya, U.S.S.R.

tu Tuamoto Islands, France

raj Rajasthan, India

ch Lop Nor, Sinkiang, China

Table A2 lists the station correction terms determined jointly along with the network m_b values.

¹ Blandford, R. R., and R. H. Shumway (1982). Magnitude:yield for nuclear explosions in granite at the Nevada Test Site and Algeria: joint determination with station effects and with data containing clipped and low-amplitude signals, *Technical Report VSC-TR-82-12*, Teledyne Geotech, Alexandria, Virginia.

² Jih, R.-S., and R. H. Shumway (1989). Iterative network magnitude estimation and uncertainty assessment with noisy and clipped data, Bull. Seismo. Soc. Am., 79, 1122-1141.

Geotech Network $\rm m_b$

Table A1. Geotech's Maximum-Likelihood Network m_b							
Event	# of Signals	$m_b(P_a)$	$m_b(P_b)$	$m_b(P_{\text{max}})$	σ		
ALMENDRO	26,0,2	5.730	6.026	6.233	0.060		
BENHAM	42,1,7	5.772	6.103	6.359	0.045		
BILBY	36,3,0	5.148	5.404	5.658	0.051		
BOURBON	18,31,0	4.587	4.720	4.904	0.046		
BOXCAR	32,0,4	5.849	6.189	6.412	0.053		
CAMBRIC	12,34,0	4.091	4.340	4.551	0.047		
CHANCELLOR	16,12,1	4.887	5.183	5.338	0.059		
CHARTREUSE	31,16,1	4.884	5.010	5.249	0.046		
CHATEAUGAY	17,28,2	4.478	4.884	5.066	0.047		
CORDUROY	18,14,0	4.971	5.092	5.287	0.057		
HANDCAR	16,33,0	4.308	4.495	4.629	0.046		
HANDLEY	41,1,1	6.062	6.307	6.480	0.049		
HARZER	31,5,1	5.011	5.312	5.536	0.053		
KANKAKEE	24,27,0	4.347	4.597	4.847	0.045		
MAST	29,1,0	5.403	5.739	5.981	0.058		
NASH	31,21,0	4.758	4.918	5.149	0.044		
PILEDRIVER	38,12,1	4.925	5.194	5.435	0.045		
REX	16,35,1	3.875	4.376	4.720	0.044		
SCOTCH	38,8,1	5.079	5.344	5.600	0.047		
CANNIKIN	49,0,20	6.408	6.663	6.911	0.039		
MILROW	52,0,4	5,945	6.195	6.494	0.043		
LONGSHOT	67,4,3	5.056	5.428	5.818	0.037		
FAULTLESS	47,1,3	5.829	6.157	6.460	0.045		
GASBUGGY	11,37,0	4.153	4.412	4.661	0.046		
RIO BLANCO	15,20,0	4.068	4.545	4.810	0.054		
RULISON	9,37,0	4.108	4.240	4.554	0.047		
SHOAL	13,27,0	4.321	4.455	4.738	0.051		
SALMON	6,33,0	3.439	3.974	4.180	0.051		

Table A1. Geotech's Maximum-Likelihood Network m _b (Continued)							
Event	# of Signals	$m_b(P_a)$	$m_b(P_b)$	$m_b(P_{\text{max}})$	σ		
azg22apr66	3,10,0	3.867	4.101	4.183	0.089		
azg22dec71	12,0,2	5.473	5.826	6.164	0.086		
azg25apr75	1,16,0		3.904	3.944	0.078		
azg29jul76	41,5,7	5.105	5.579	5.864	0.044		
azg30sep77	21,30,1	4.049	4.588	4.828	0.044		
azg17oct78	7,0,5	5.271	5.724	6.097	0.092		
azg18dec78	9,0,3	5.374	5.748	6.119	0.092		
azg17jan79	10,0,4	5.515	5.869	6.153	0.086		
azg14jul79	10,0,1	4.831	5.371	5.699	0.097		
azg24oct79	3,0,6	4.848	5.681	5.960	0.107		
pne29aug74	27,18,0	3.994	4.397	4.722	0.048		
mek18dec66	55,9,1	5.261	5.493	5.709	0.040		
dek21nov65	48,15,1	4.875	5.152	5.362	0.040		
dek13feb66	51,4,10	5.640	5.890	6.082	0.040		
dek20mar66	50,9,8	5.335	5.624	5.850	0.039		
dek07may66	9,26,1	3.992	4.233	4.486	0.053		
dek26feb67	48,9,6	5.353	5.597	5.821	0.040		
dek29sep68	50,8,6	5.125	5.432	5.627	0.040		
dek23jul69	38,21,1	4.594	4.920	5.167	0.041		
dek11sep69	19,39,0	3.975	4.234	4.576	0.042		
dek25apr71	37,5,0	5.299	5.566	5.756	0.049		
dek30dec71	16,3,0	4.982	5.347	5.524	0.073		
dek28mar72	28,17,0	4.351	4.726	4.959	0.048		
dek16aug72	24,23,1	4.337	4.620	4.885	0.046		
dek10dec72	30,7,5	4.975	5.333	5.532	0.049		
dek29mar77	25,14,0	4.304	4.700	4.981	0.051		
dek30jul77	21,16,0	4.200	4.604	4.857	0.053		
dek26mar78	25,6,0	4.948	5.272	5.497	0.057		
dek22apr78	21,9,0	4.466	4.765	5.014	0.058		

Event # of Signals $m_b(P_a)$ $m_b(P_b)$ $m_b(P_{max})$ σ sek15jan65 46,1,2 5.493 5.732 5.880 0.046 sek19jun68 28,3,2 4.618 5.000 5.261 0.056 sek30nov69 32,0,0 5.378 5.767 5.975 0.057 sek30juh71 31,19,1 4.470 4.766 5.038 0.045 sek10feb72 34,8,2 4.803 5.071 5.304 0.048 sek02nov72 29,1,15 5.590 5.938 6.187 0.046 sek10dec72 29,2,11 5.784 6.013 0.049 sek23jul73 38,1,1 5.753 5.996 6.181 0.051 sek14dec73 45,8,6 5.245 5.545 5.770 0.042 sek27apr75 18,1,1 4.904 5.242 5.491 0.072 sek04jul76 14,0,5 5.229 5.598 5.927 0.073 sek15sep78 30,1,5
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sek23jun79 38,3,3 5.615 5.846 6.049 0.048 sek14sep80 29,5,6 5.439 5.752 5.987 0.051 nnz27oct66 56,0,14 6.063 6.295 6.436 0.038 nnz21oct67 53,5,3 5.400 5.590 5.765 0.041 nnz07nov68 59,1,5 5.580 5.831 6.025 0.040 nnz14oct69 59,2,7 5.760 5.957 6.129 0.039 nnz14oct70 35,0,22 6.424 6.633 6.813 0.042
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nnz27oct66 56,0,14 6.063 6.295 6.436 0.038 nnz21oct67 53,5,3 5.400 5.590 5.765 0.041 nnz07nov68 59,1,5 5.580 5.831 6.025 0.040 nnz14oct69 59,2,7 5.760 5.957 6.129 0.039 nnz14oct70 35,0,22 6.424 6.633 6.813 0.042
nnz21oct67 53,5,3 5.400 5.590 5.765 0.041 nnz07nov68 59,1,5 5.580 5.831 6.025 0.040 nnz14oct69 59,2,7 5.760 5.957 6.129 0.039 nnz14oct70 35,0,22 6.424 6.633 6.813 0.042
nnz07nov68 59,1,5 5.580 5.831 6.025 0.040 nnz14oct69 59,2,7 5.760 5.957 6.129 0.039 nnz14oct70 35,0,22 6.424 6.633 6.813 0.042
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nnz14oct70 35,0,22 6.424 6.633 6.813 0.042
nnz27sep71 23,0,21 6.259 6.475 6.619 0.048
nnz28aug72 32,0,11 5.989 6.247 6.371 0.049
nnz12sep73 23,0,21 6.347 6.672 6.763 0.048
nnz29aug74 25,0,18 6.126 6.394 6.578 0.049
nnz21oct75 23,0,17 6.095 6.333 6.541 0.051
nnz23aug75 28,0,12 6.112 6.367 6.488 0.051
nnz20oct76 25,34,1 4.031 4.350 4.659 0.041
nnz01sep77 26,2,2 5.099 5.415 5.561 0.058
nnz10aug78 39,3,18 5.392 5.625 5.856 0.041

Table A1. Geotech's Maximum-Likelihood Network m_b (Continued)							
Event	# of Signals	$m_b(P_a)$	$m_b(P_b)$	$m_b(P_{\text{max}})$	σ		
nnz11oct80	42,4,6	5.181	5.442	5.658	0.044		
nnz01oct81	43,4,5	5.226	5.489	5.649	0.044		
nnz18aug83	30,5,5	5.321	5.526	5.703	0.051		
nnz25oct84	22,3,4	5.154	5.427	5.599	0.059		
snz27sep73	32,3,1	5.196	5.490	5.729	0.053		
snz27oc73a	14,0,24	6.647	6.873	7.092	0.052		
snz27oc73b	9,28,0	_	3.999	4.150	0.053		
snz27oc73c	4,34,0	3.544	3.886	3.908	0.052		
snz02nov74	12,0,29	6.497	6.790	7.012	0.050		
snz18oct75	21,0,21	6.227	6.518	6.834	0.049		
BERYL	11,6,0	4.412	4.778	4.985	0.078		
CORUNDON	11,42,0	3.797	3.899	4.212	0.044		
EMERAUDE	14,25,0		4.261	4.566	0.051		
GRENAT	32,32,1	4.292	4.494	4.763	0.040		
OPALE	3,51,0	3.770	3.855	3.896	0.044		
RUBIS	42,5,0	4.826	5.167	5.429	0.047		
SAPHIR	52,5,5	5.182	5.464	5.716	0.041		
TOURMALINE	27,39,0	4.106	4.427	4.644	0.039		
TURQOISE	11,55,0		3.941	4.221	0.039		
tu19feb77	16,28,0		4.370	4.622	0.048		
tu19mar77	20,6,1	5.141	5.438	5.639	0.062		
tu24nov77	33,0,0	5.051	5.369	5.662	0.056		
tu25jul79	18,0,0	5.090	5.570	5.864	0.075		
tu23mar80	27,14,3	4.677	5.105	5.358	0.048		
tu 19jul80	38,2,2	4.891	5.158	5.513	0.049		
tu03dec80	32,11,0	4.689	4.981	5.331	0.049		
tu25jul82	22,13,0	4.675	5.034	5.210	0.054		
tu19apr83	22,1,0	4.993	5.199	5.495	0.067		

Table A1. Geotech's Maximum-Likelihood Network m_b (Continued)							
Event	# of Signals	$m_b(P_a)$	$m_b(P_b)$	$m_b(P_{\rm max})$	σ		
tu25may83	18,0,0	5.150	5.455	5.785	0.075		
tu30nov78	40,7,2	4.820	5.234	5.611	0.046		
raj18may74	7,23,0	4.022	4.303	4.563	0.058		
ch22sep69	30,12,0	4.325	4.742	5.133	0.049		
ch27oct75	12,24,0	4.131	4.396	4.585	0.053		
ch17oct76	13,33,0	3.884	4.146	4.532	0.047		
ch06oct83	17,13,1	4.769	5.029	5.243	0.057		
ch03oct84	10,12,0	4.453	4.747	4.999	0.068		
ch19dec84	3,10,0	4.017	3.999	4.381	0.089		

	Table A2. WWSSN Station Corrections						
Code	# of Signals	Site Term	Longitude	Latitude	Description		
AAE	78,93,17	-0.243±0.023	38.765556	9.029166	Addis Ababa, Ethiopia		
AAM	134,64,6	0.254±0.022	-83.656113	42.299721	Ann Arbor, Michigan		
ADE	16,25,0	0.001±0.050	138.708893	-34.966946	Adelaide, Australia		
AFI	27,65,0	-0.143±0.033	-171.777252	-13.909333	Afiamalu, Samoa Islands		
AKU	71,69,0	-0.093±0.027	-18.106667	65.686668	Akureyri, Iceland		
ALQ	99,15,19	0.039±0.028	-106.457497	34.942501	Albuquerque, New Mexico		
ANP	20,67,0	-0.327±0.034	121.516670	25.183332	Anpu, Formosa		
ANT	41,49,2	0.056±0.033	-70.415276	-23.705000	Antofagasta, Chile		
AQU	66,44,13	-0.054±0.029	13.403055	42.353889	Aquila, Italy		
ARE	83,40,0	0.101±0.029	-71.491280	-16.462084	Arequipa, Peru		
ASP	1,2,0	-0.581±0.185	133.896667	-23.683332	Alice Springs, Australia		
ATL	79,19,2	0.164±0.032	-84.337502	33.433334	Atlanta, Georgia		
ATU	112,78,16	0.146±0.022	23.716667	37.972221	Athens Univ., Greece		
BAG	132,68,8	-0.028±0.022	120.579720	16.410833	Baguio City, Philippine Islands		
BDF	10,2,0	-0.009±0.092	-47.903332	-15.663834	Brasilia array, Brazil		
BEC	45,102,3	-0.131±0.026	-64.681114	32.379444	Bermuda-Columbia, Atlantic Ocean		
ВНР	30,75,0	-0.176±0.031	-79.558052	8.960834	Balboa Heights, Panama		
BKS	141,65,1	0.087±0.022	-122.235001	37.876667	Byerly, California		
BLA	152,53,12	0.122±0.022	-80.420998	37.211304	Blacksburg, West Virginia		
BOG	41,76,0	0.057±0.030	-74.065002	4.623055	Bogota, Colombia		
BOZ	44,4,5	0.238±0.044	-111.633331	45.599998	Bozeman, Montana		
BUL	149,34,9	0.049±0.023	28.613333	-20.143333	Bulawayo, Rhodesia		
CAR	92,59,7	0.154±0.025	-66.927635	10.506667	Caracas, Venezuela		
CCG	1,0,0	-0.186±0.320	-61.133335	77.166664	Camp Century, Greenland		
CHG	97,16,36	-0.127±0.026	98.976944	18.790001	Chiengmai, Asia		
CMC	50,27,0	-0.140±0.036	-115.083336	67.833336	Copper Mine, Canada		
COL	259,47,28	0.087±0.018	-147.793335	64.900002	College Outposta, Alaska		
COP	74,101,14	0.166±0.023	12.433333	55.683334	Copenhagen, Denmark		
COR	77,59,3	0.111±0.027	-123.303192	44.585724	Corvallis, Oregon		
CTA	57,16,4	0.214±0.036	146.254440	-20.088333	Charters Towers, Australia		

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	Table A2. WWSSN Station Corrections (Continued)						
Code	# of Signals	Site Term	Longitude	Latitude	Description		
DAG	21,13,5	0.001±0.051	-18.770000	76.769997	Danmarkshavn, Greenland		
DAL	17,24,4	0.191±0.048	-96.783890	32.846111	Dallas, Texas		
DAV	24,81,0	-0.276±0.031	125.574722	7.087778	Davao, Philippine Islands		
DUG	170,17,29	0.075±0.022	-112.813332	40.195000	Dugway, Utah		
EIL	25,3,43	0.075±0.038	34.950001	29.549999	Eilat, United Arab Republic		
EPT	29,2,2	0.005±0.056	-106.505836	31.771667	El Paso, Texas-Mexico border		
ESK	88,80,2	0.117±0.025	-3.205000	55.316666	Eskdalemuir, United Kingdom		
FLO	80,20,9	0.064±0.031	-90.370003	38.801666	Florissant, Missouri		
FVM	44,8,0	-0.008±0.044	-90.426003	37.984001	French Village, Missouri		
GDH	154,126,1	-0.159±0.019	-53.533333	69.250000	Godhavn, Greenland		
GEO	88,69,2	0.021±0.025	-77.066666	38.900002	Georgetown, Virginia		
GIE	9,38,0	-0.188±0.047	-90.300003	-0.733333	Galapagos Islands		
GOL	157,24,11	-0.216±0.023	-105.371109	39.700279	Golden, Colorado		
GRM	1,20,0	-0.093±0.070	26.573334	-33.313332	Grahamstown, South Africa		
GSC	89,22,16	0.089±0.028	-116.804611	35.301666	Goldstone, California		
GUA	78,175,0	-0.250±0.020	144.911667	13.538333	Guam, Mariana Islands		
нкс	85,84,0	-0.131±0.025	114.171890	22.303556	Hong Kong		
HLW	47,36,32	-0.047±0.030	31.341667	29.858334	Helwan, United Arab Republic		
HNR	30,92,0	0.188±0.029	159.947113	-9.432195	Honiara, Solomon Islands		
HON	6,9,0	0.051±0.083	-158.008331	21.321667	Honolulu, Hawaii		
ном	1,10,0	0.258±0.097	88.309166	22.416666	Howrah, India-Bangladesh border		
IST	102,79,25	0.186±0.022	28.995832	41.045555	Istanbul, Turkey		
JCT	59,4,24	0.159±0.034	-99.802223	30.479445	Junction City, Texas		
JER	89,45,25	0.039±0.025	35.197224	31.771944	Jerusalem, Dead Sea		
KBL	14,0,46	0.142±0.041	69.043167	34.540833	Kabul, Afghanistan		
KBS	55,40,0	-0.181±0.033	11.923889	78.917503	Kingsbay, Svalbard		
KEV	121,102,4	-0.123±0.021	27.006666	69.755280	Kevo, Finland		
KIP	84,153,0	0.107±0.021	-158.014999	21.423334	Kipapa, Hawaii		
KOD	107,33,30	0.100±0.025	77.466667	10.233334	Kodaikanal, India		
KON	129,65,70	0.102±0.020	9.598222	59.649082	Kongsberg, Norway		

	Table A2. WWSSN Station Corrections (Continued)						
Code	# of Signals	Site Term	Longitude	Latitude	Description		
KRK	8,7,0	-0.171±0.083	30.062500	69.724167	Kirkenes, Norway-USSR border		
KTG	72,75,1	-0.247±0.026	-21.983334	70.416664	Kap Tobin, Greenland		
LAH	5,17,3	0.428±0.064	74.333336	31.549999	Lahore, India-Pakistan border		
LEM	54,82,0	-0.531±0.027	107.616669	-6.833333	Lembang, Java		
LON	162,44,21	-0.034±0.021	-121.809998	46.750000	Longmire, Washington		
LOR	74,8,16	0.154±0.032	3.851389	47.266666	Lormes, France		
LPA	8,91,0	0.426±0.032	-57.931946	-34.908890	La Plata, Uruguay		
LPB	58,39,3	-0.043±0.032	-68.098358	-16.532667	La Paz, Peru-Bolivia border		
LPS	50,27,3	-0.071±0.036	-89.161942	14.292222	La Palma, Quatemala		
LUB	40,30,3	0.214±0.037	-101.866669	33.583332	Lubbock, Texas		
MAL	87,41,10	0.055±0.027	-4.411111	36.727501	Malaga, straits of Gibraltar		
MAN	30,14,1	0.316±0.048	121.076859	14.662000	Manila, Philippine Islands		
MAT	145,53,25	-0.112±0.021	138.206665	36.541668	Matsushiro, Japan		
MDS	39,19,0	-0.032±0.042	-89.760002	43.372223	Madison, Wisconsin		
MHI	5,2,2	0.358±0.107	59.494499	36.299999	Meshed, Iran-USSR border		
MNN	8,6,2	0.179±0.080	-93.190002	44.914444	Minneapolis, Minnesota		
MSH	31,19,9	0.226±0.042	59.587776	36.311111	Meshed, Iran-USSR border		
MSO	46,7,2	0.061±0.043	-113.940552	46.829166	Missoula, Montana		
MUN	39,41,0	0.015±0.036	116.208336	-31.978333	Mundaring, Australia		
NAI	115,46,9	-0.089±0.025	36.803665	-1.273944	Nairobi, Kenya		
NAT	27,27,0	0.070±0.044	-35.033333	-5.116667	Natal, Brazil		
NDI	129,24,25	0.124±0.024	77.216667	28.683332	New Delhi, India		
NHA	12,3,0	-0.127±0.083	109.211670	12.210000	Nhatranga, Asia		
NIL	14,6,18	-0.008±0.052	73.251663	33.650002	Nilore, Pakistan		
NNA	47,57,0	-0.162±0.031	-76.842140	-11.987556	Nana, Peru		
NOR	78,50,3	-0.260±0.028	-16.683332	81.599998	Nord, Greenland		
NUR	103,82,7	0.051±0.023	24.651417	60.508999	Nurmijarvi, Finland		
OGD	135,63,6	-0.119±0.022	-74.595833	41.087502	Ogdensburg, New York		
OXF	79,10,17	0.347±0.031	-89.409164	34.511806	Oxford, Mississippi		
PDA	31,103,3	0.050±0.027	-25.663334	37.746666	Ponta Delgada, Azores Islands		

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Code			Table A2. WWSSN Station Corrections (Continued)						
	# of Signals	Site Term	Longitude	Latitude	Description				
PEL	29,39,3	0.052±0.038	-70.685280	-33.143612	Peldehue, Chile-Argentina				
PMG	82,58,2	-0.005±0.027	147.153885	-9.409166	Port Moresby, New Guinea				
POO	133,40,28	0.037±0.023	73.849998	18.533333	Pcona, India				
PRE	65,42,0	-0.074±0.031	28.190001	-25.753334	Pretoria, South Africa				
PTO	84,52,5	-0.140±0.027	-8.602222	41.138611	Porto Serro Do, Portugal				
QUE	82,23,41	-0.412±0.026	66.949997	30.188334	Quetta, Pakistan				
QUI	9,67,0	0.007±0.037	-78.500504	-0.200139	Quito, Ecuador				
RAB	45,135,0	-0.177±0.024	152.169830	-4.191278	Rabaul, New Britain				
RAR	12,30,0	-0.070±0.049	-159.773331	-21.212500	Rarotonga, Cook Islands				
RCD	28,22,3	0.439±0.044	-103.208336	44.075001	Rapid City, South Dakota				
RIV	9,22,0	0.355±0.057	151.158340	-33.829361	Riverview, Australia				
SBA	2,12,0	-0.619±0.086	166.756104	-77.850281	Scott Base, Antarctica				
SCP	167,68,21	0.055±0.020	-77.864998	40.794998	State College, Pennsylvania				
SDB	75,17,9	0.083±0.032	13.571944	-14.925834	Sa Da Bandeira, Angola				
SEO	97,76,12	-0.076±0.024	126.966667	37.566666	Seoul Keizyo, South Korea				
SHA	76,65,0	0.346±0.027	-88.142807	30.694361	Spring Hill, Mississippi				
SHI	77,14,30	0.298±0.029	52.519943	29.638306	Shiraz, Iran				
SHK	41,76,0	-0.324±0.030	132.677505	34.532223	Shiraki, Honshu, Japan				
SHL	83,15,41	0.033±0.027	91.883331	25.566668	Shillong, India-Bangladesh border				
SJG	129,57,0	-0.248±0.023	-66.150002	18.111666	San Juan, Puerto Rico				
SNA	6,11,0	0.108±0.078	-2.325000	-70.315002	Sanae, Antarctica				
SNG	44,31,3	-0.072±0.036	100.620003	7.173333	Songkhla, Malay Peninsula				
SPA	13,7,0	-0.756±0.072	0.000000	-90.000000	South Pole, Antarctica				
STU	172,94,20	0.094±0.019	9.195000	48.771946	Stuttgart, Germany				
TAB	76,53,5	0.216±0.028	46.326668	38.067501	Tabriz, Iran-USSR border				
TAU	12,14,0	-0.115±0.063	147.320419	-42.909916	Tasmania Univ., Tasmania				
TOL	112,52,23	0.211±0.023	-4.048611	39.881390	Toledo, Spain				
TRI	128,85,25	-0.105±0.021	13.764167	45.708889	Trieste, Italy				
TRN	112,70,1	0.101±0.024	-61.402779	10.648916	Trinidad, Trinidad				
	57,3,21	0.077±0.036	-110.782219	32.309723	Tucson, Arizona				

Table A2. WWSSN Station Corrections (Continued)							
# of Signals	Site Term	Longitude	Latitude	Description			
123,53,2	0.170±0.024	20.236666	63.814999	Umea, Sweden			
10,13,1	-0.236±0.065	-99.178085	19.329000	Nat. University of Central Mexico			
2,1,0	-0.261±0.185	-79.533997	8.981500	Univ. de Panama, Panama			
122,122,12	0.015±0.020	-10.244166	51.939445	Valentia Eire			
8,12,0	0.139±0.072	174.768326	-41.286110	Wellington, New Zealand			
135,118,6	-0.139±0.020	-71.322083	42.384693	Weston, New England			
32,29,0	-0.186±0.041	17.100000	-22.566668	Windhoek, South-West Africa			
	123,53,2 10,13,1 2,1,0 122,122,12 8,12,0 135,118,6	# of Signals Site Term 123,53,2 0.170±0.024 10,13,1 -0.236±0.065 2,1,0 -0.261±0.185 122,122,12 0.015±0.020 8,12,0 0.139±0.072 135,118,6 -0.139±0.020	# of Signals Site Term Longitude 123,53,2 0.170±0.024 20.236666 10,13,1 -0.236±0.065 -99.178085 2,1,0 -0.261±0.185 -79.533997 122,122,12 0.015±0.020 -10.244166 8,12,0 0.139±0.072 174.768326 135,118,6 -0.139±0.020 -71.322083	# of Signals Site Term Longitude Latitude 123,53,2 0.170±0.024 20.236666 63.814999 10,13,1 -0.236±0.065 -99.178085 19.329000 2,1,0 -0.261±0.185 -79.533997 8.981500 122,122,12 0.015±0.020 -10.244166 51.939445 8,12,0 0.139±0.072 174.768326 -41.286110 135,118,6 -0.139±0.020 -71.322083 42.384693			

Geotech Network $\rm m_b$

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